

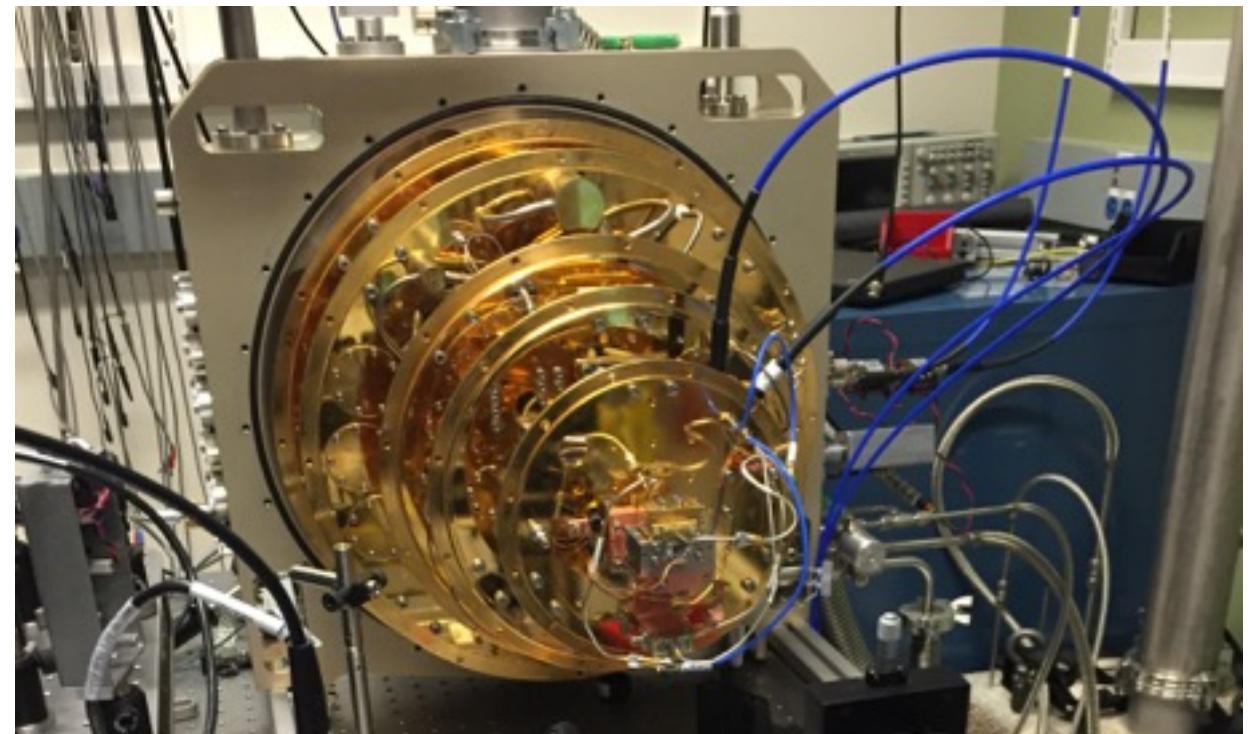
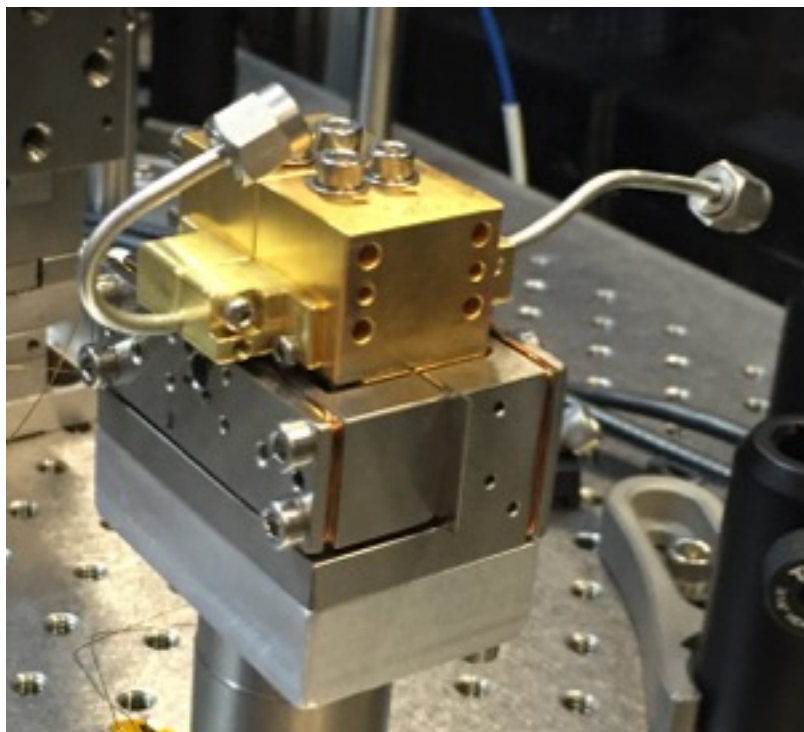
Microwave-mechanical-optical transducer in a dilution refrigerator

Electromechanics

Andrew Higginbotham
Pete Burns
Tim Menke
Konrad Lehnert

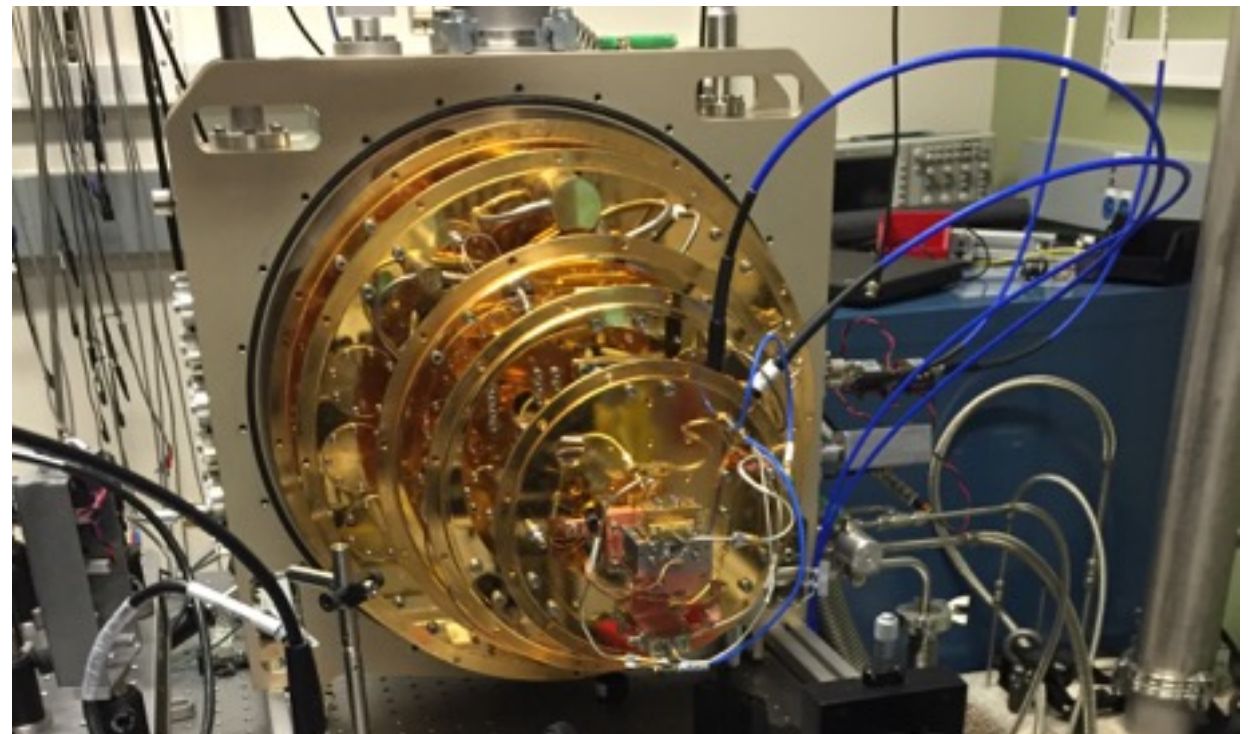
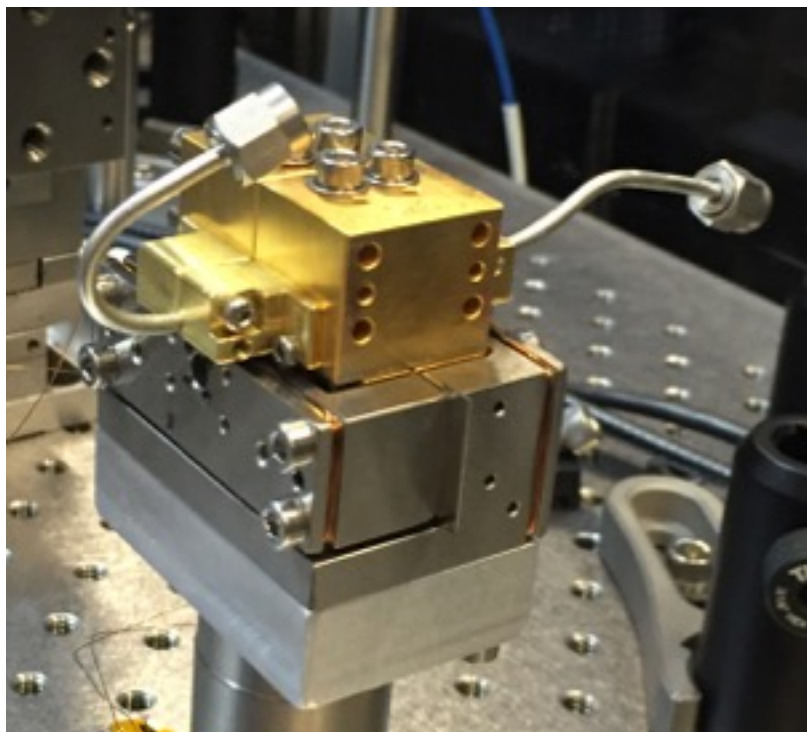
Optomechanics

Bob Peterson
Max Urmey
Nir Kampel
Cindy Regal

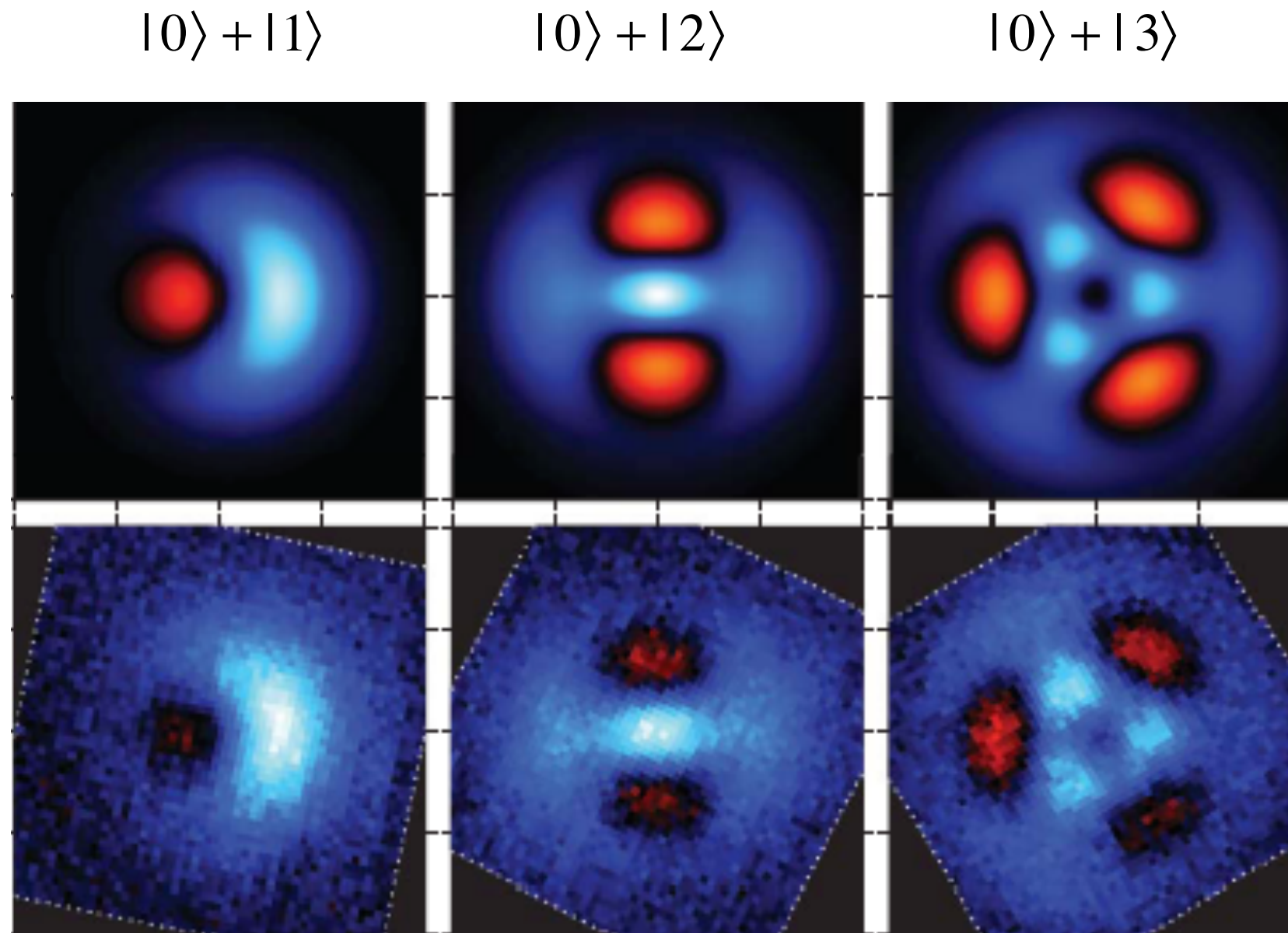


Outline

- Review of classical converter at 4 K
- Classical conversion at 100 mK 
- Projections for microwave-optical entanglement



Flexible control of microwave photons with superconducting circuits



Hofheinz...Martinis, Cleland, Nature (2009)

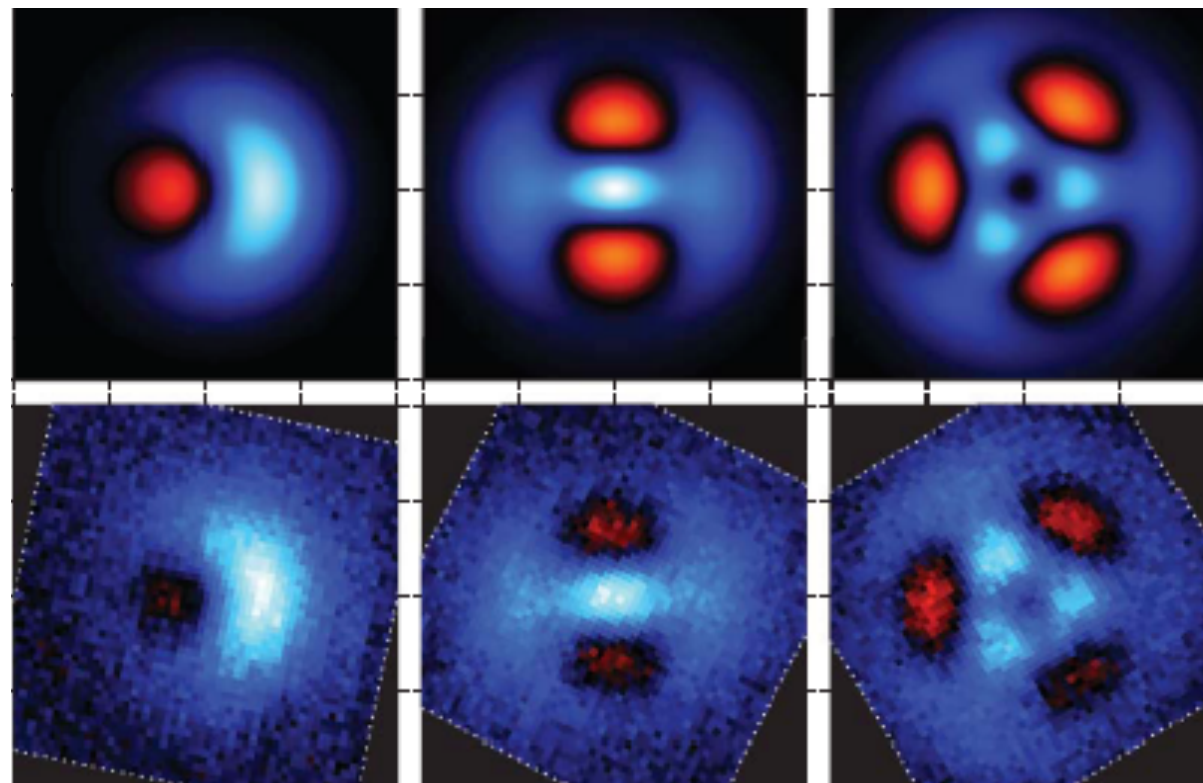
Flexible control of microwave photons with superconducting circuits

cryostat - 50 mK

$|0\rangle + |1\rangle$

$|0\rangle + |2\rangle$

$|0\rangle + |3\rangle$

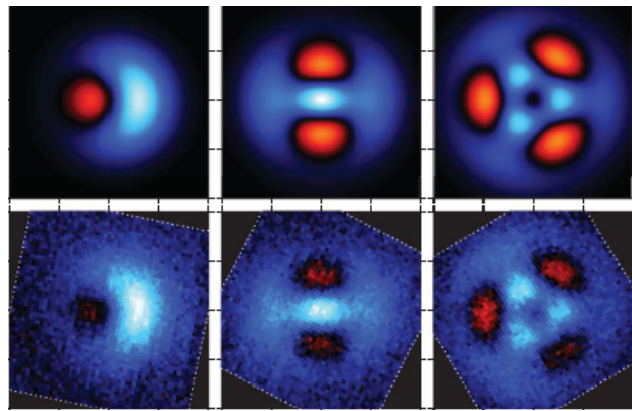


Hofheinz...Martinis, Cleland, Nature (2009)

$$\frac{\hbar\omega}{k_b} \sim 0.3 \text{ K}, T_c \sim 1 \text{ K}$$

How can we plug-in to superconducting qubits?

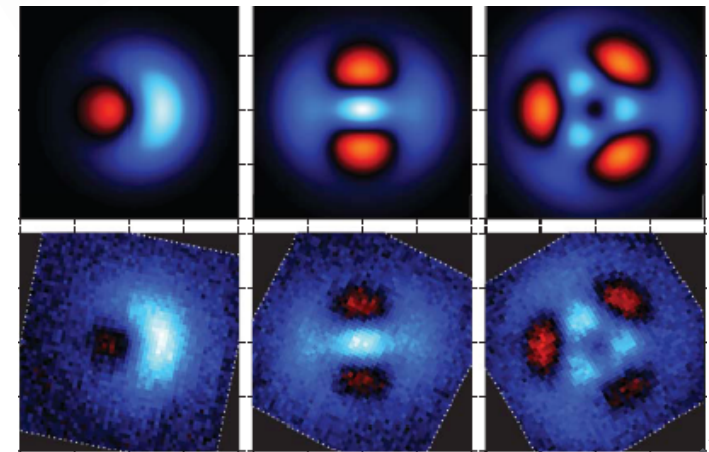
cryostat - 50 mK



$$\frac{\hbar\omega}{k_B} \sim 0.3 \text{ K}$$

optical network - 300 K

cryostat - 50 mK



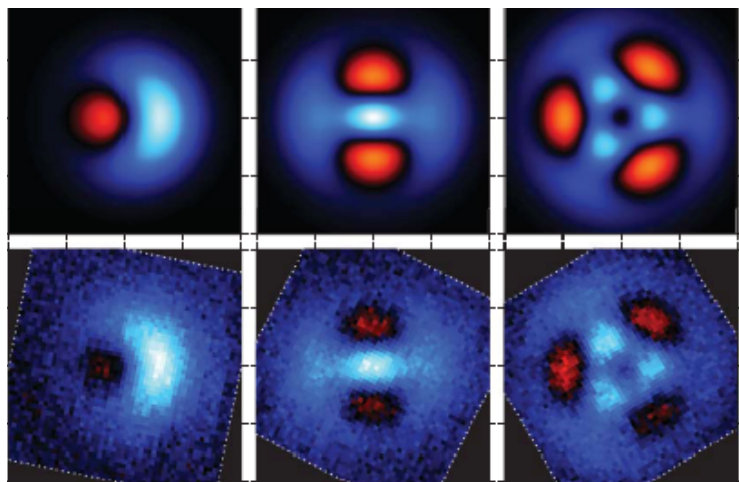
$$\frac{\hbar\omega}{k_B} \sim 0.3 \text{ K}$$

$$\frac{\hbar\omega}{k_B} \sim 10^4 \text{ K}$$

Our approach: low-frequency mechanical oscillators

microwave

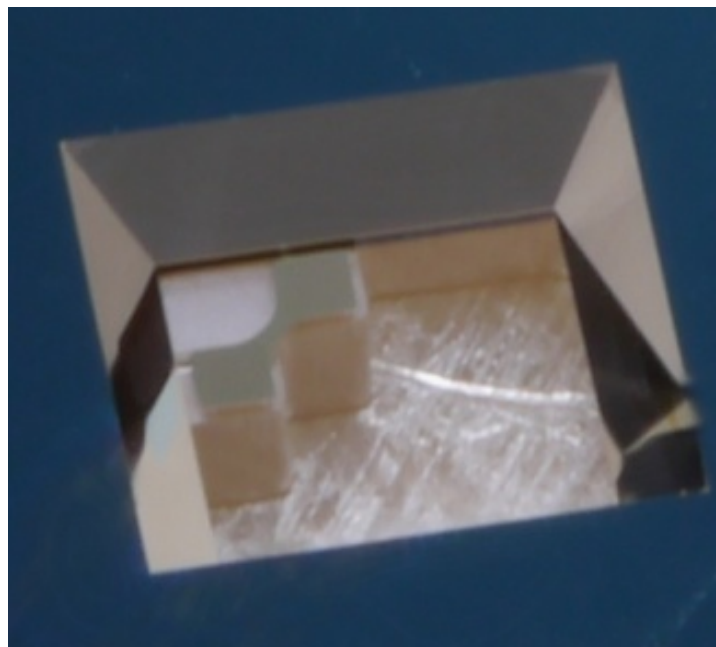
$$\frac{\hbar\omega}{k_b} \sim 0.3 \text{ K}$$



Hofheinz...Martinis, Cleland, Nature (2009)

mechanical

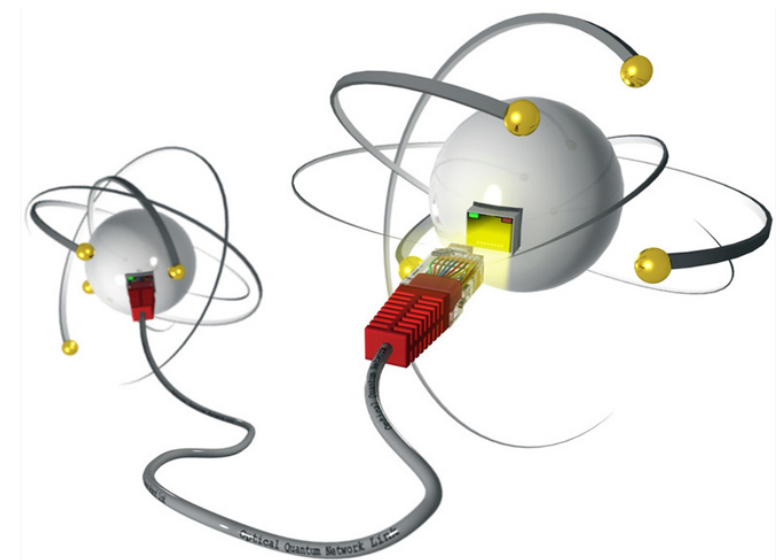
$$\frac{\hbar\omega}{k_b} \sim 50 \mu\text{K}$$



$$n_{\text{th}}\gamma_m = 2\pi \times 8 \text{ kHz}$$

optical

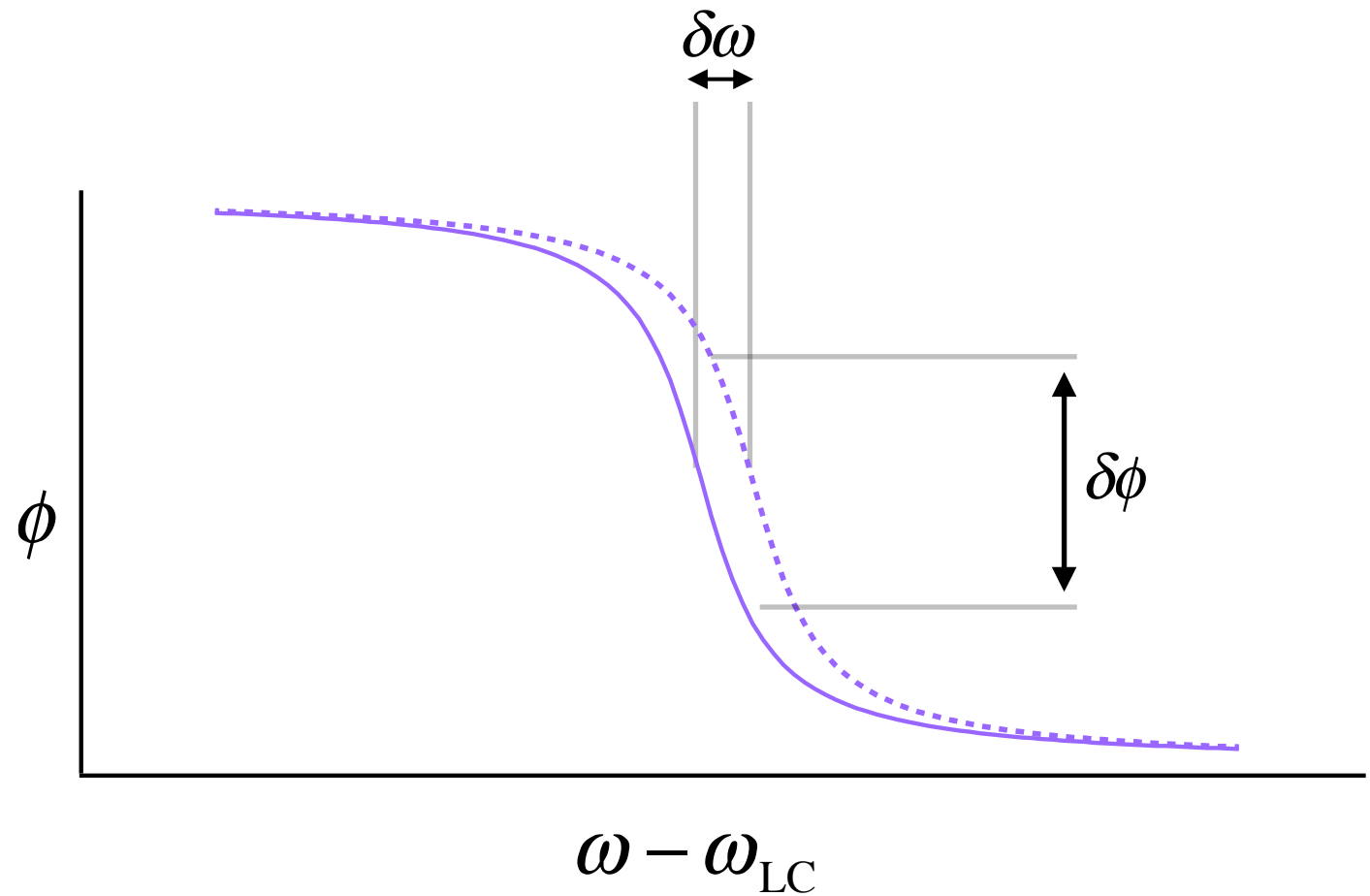
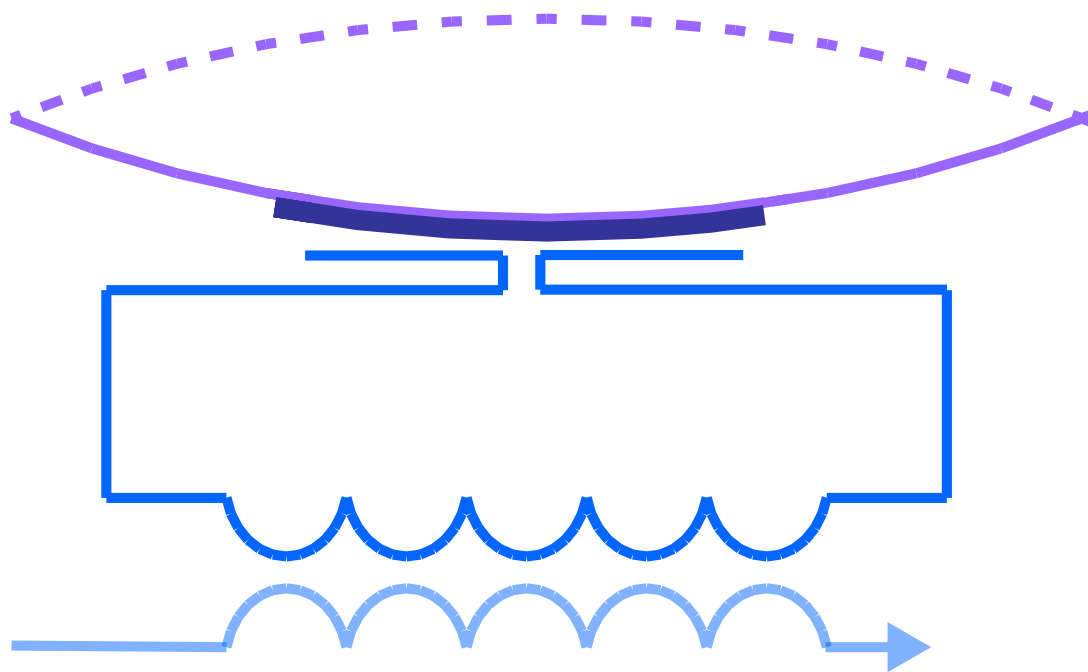
$$\frac{\hbar\omega}{k_b} \sim 10^4 \text{ K}$$



Ritter...Rempe, Nature (2012)

Electromechanics interaction:

Static mechanical displacement causes phase shifts

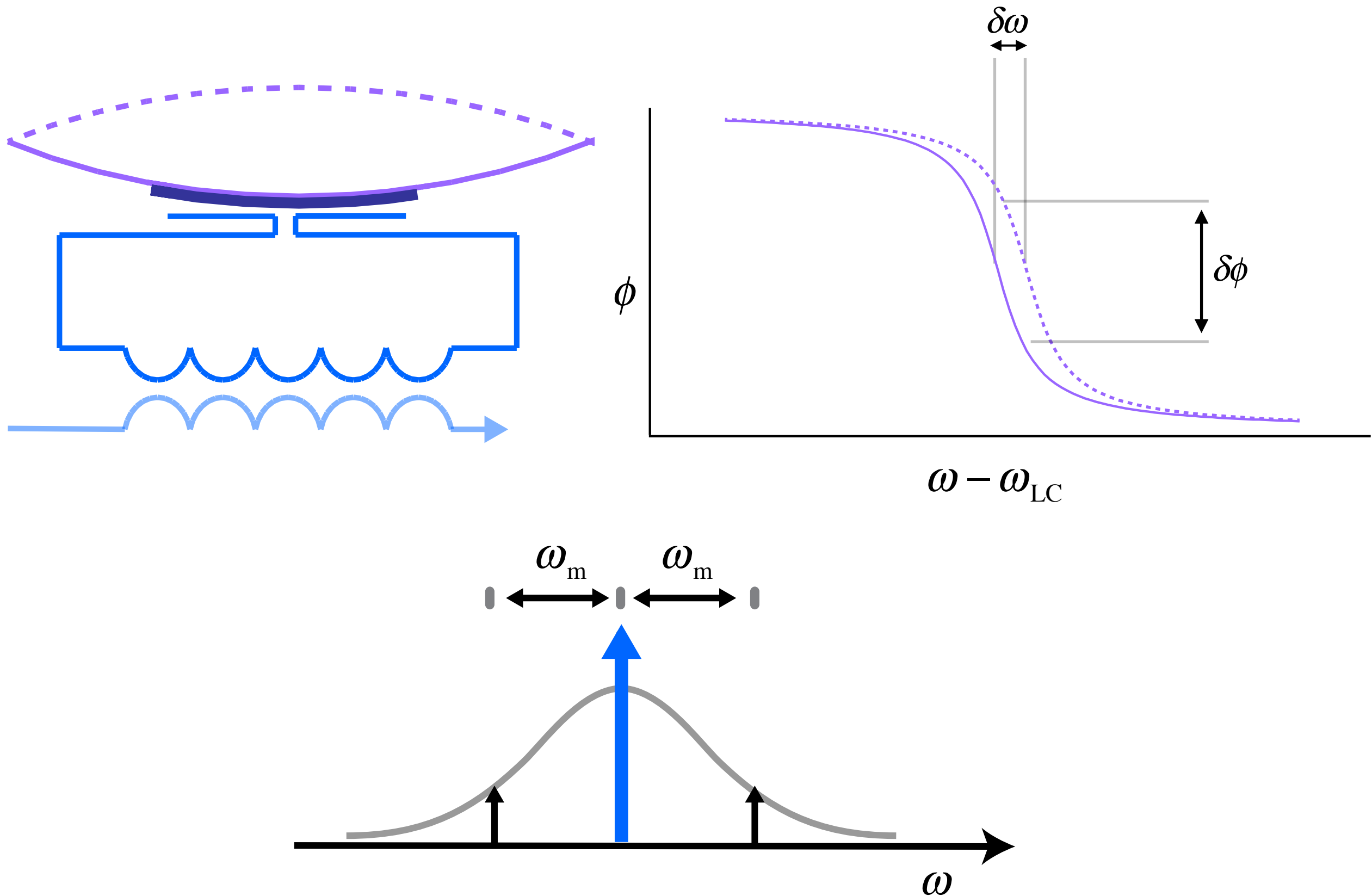


$$\omega = \frac{1}{\sqrt{LC}}$$

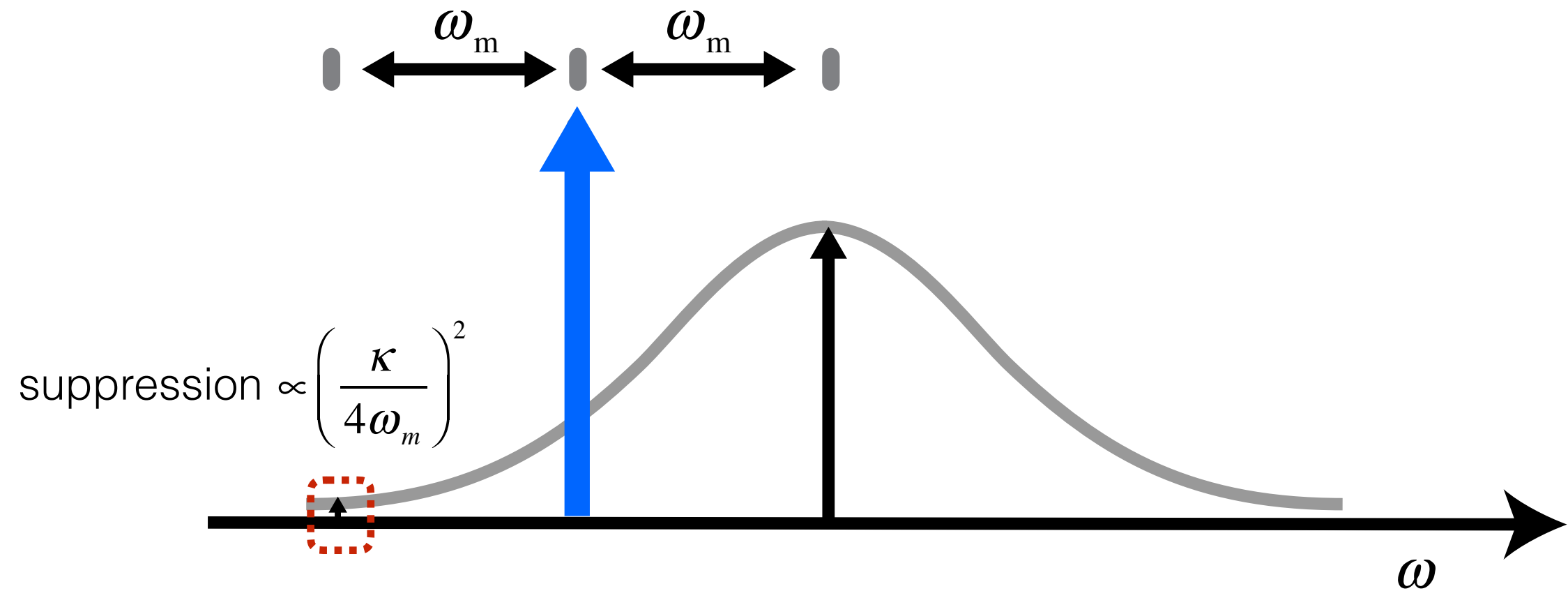
$$\delta\omega = \frac{d\omega}{dC} \delta C$$

Electromechanics:

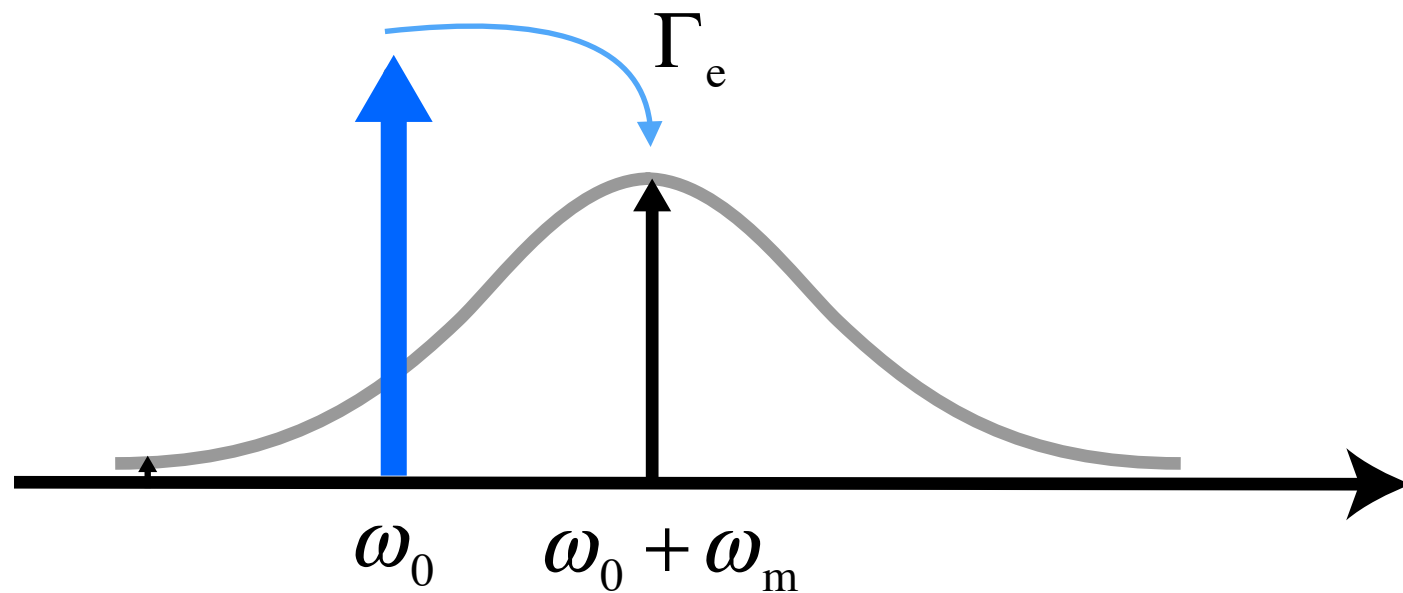
Oscillating displacement causes PM sidebands



Selecting a sideband with cavity density of states

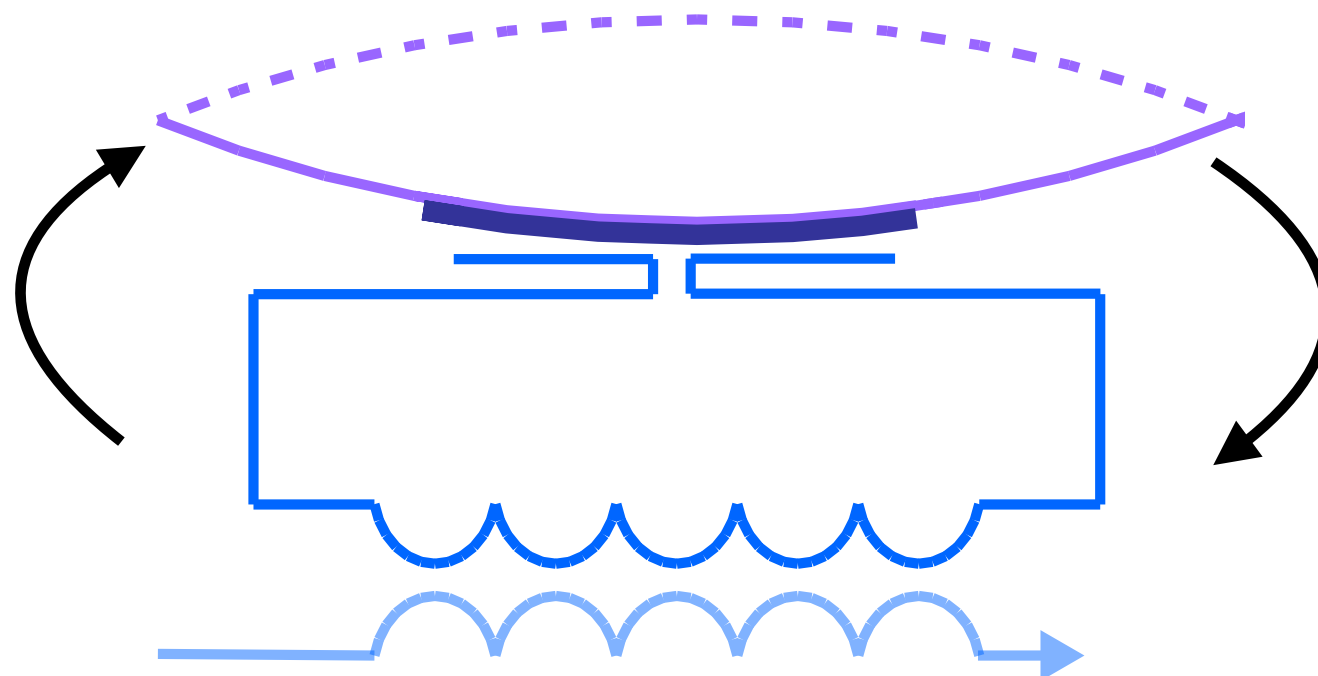


Energetics of the upper sideband: swapping photons and phonons



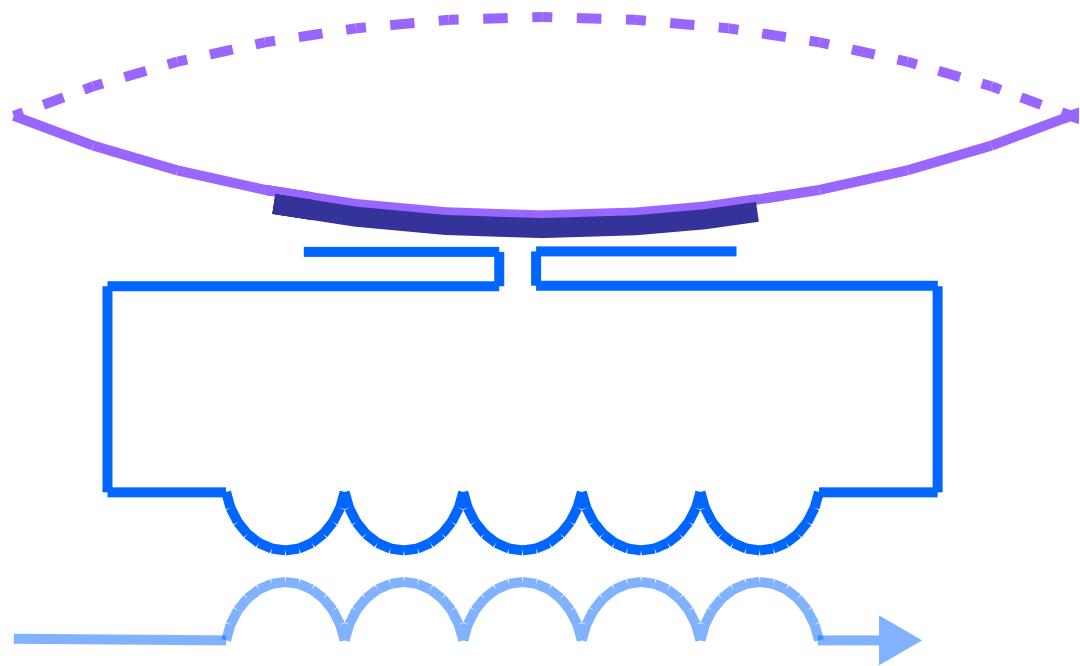
$$H_{\text{int}} = \hbar g_0 a_{\text{mw}}^\dagger a_{\text{mech}} + \text{h.c.}$$

generates mech-mw swaps



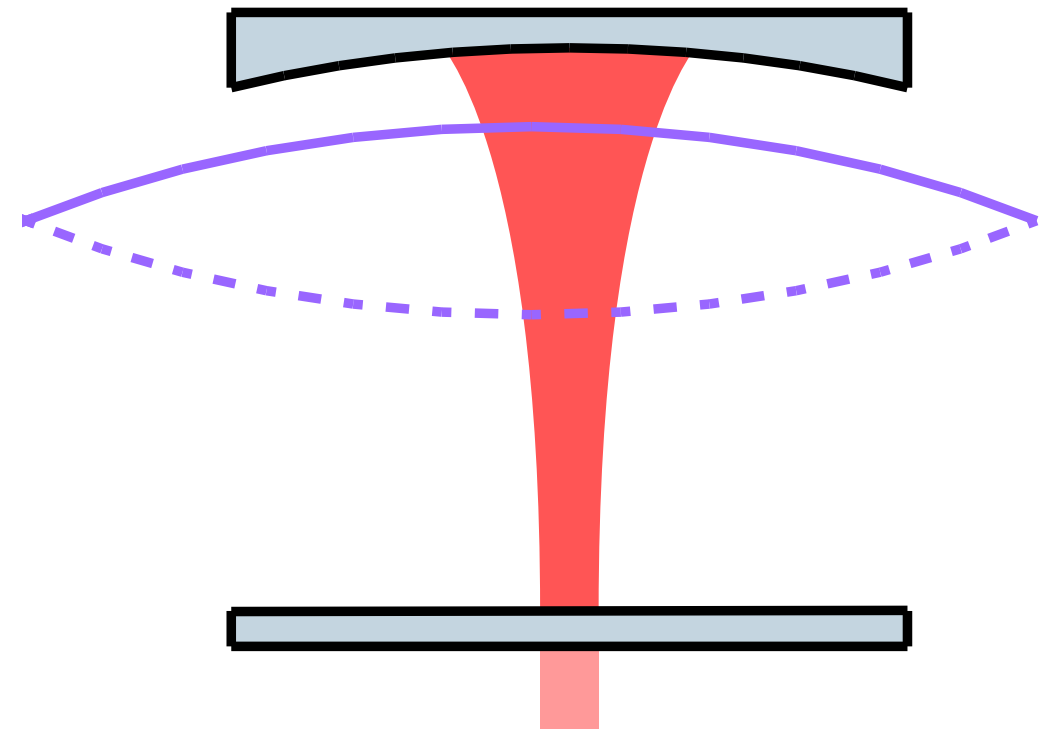
Microwave-mechanical-optical strategy for state transduction

microwave $\longleftrightarrow$ mechanics



Lehnert group

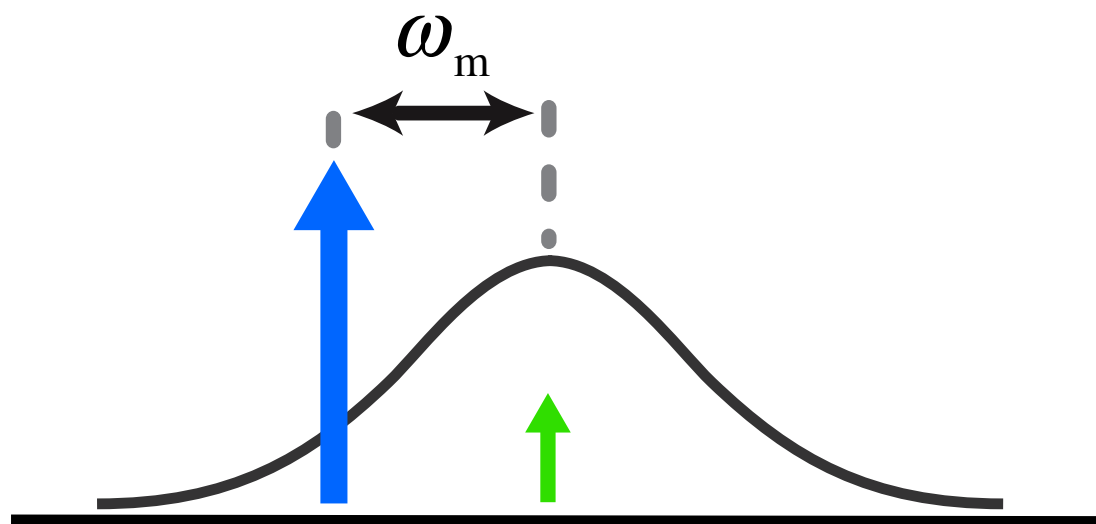
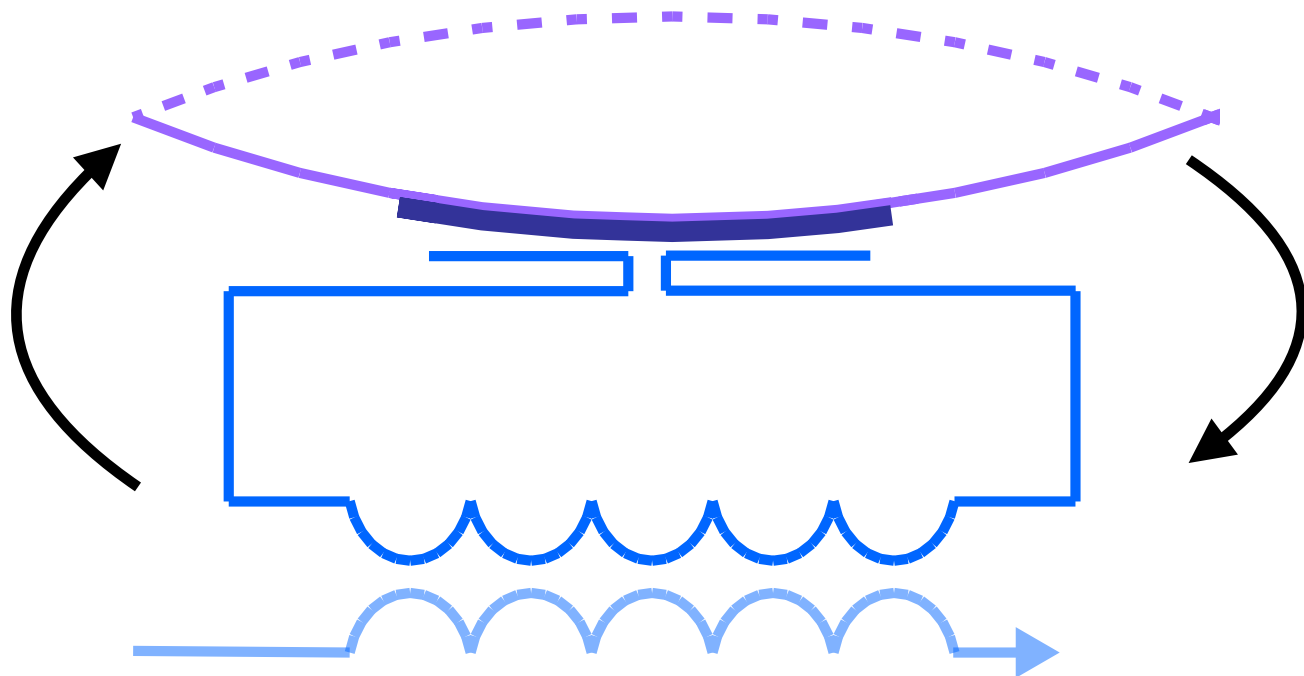
mechanics $\longleftrightarrow$ optics



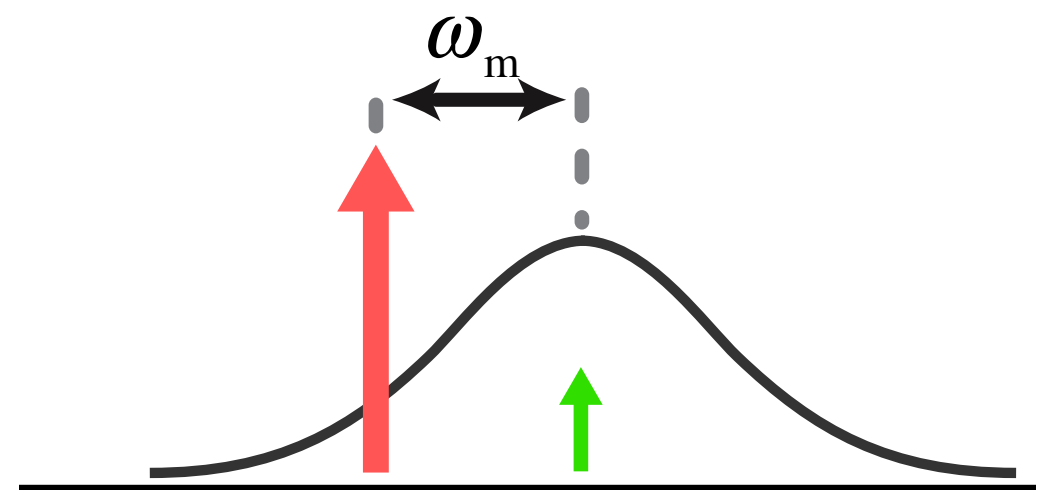
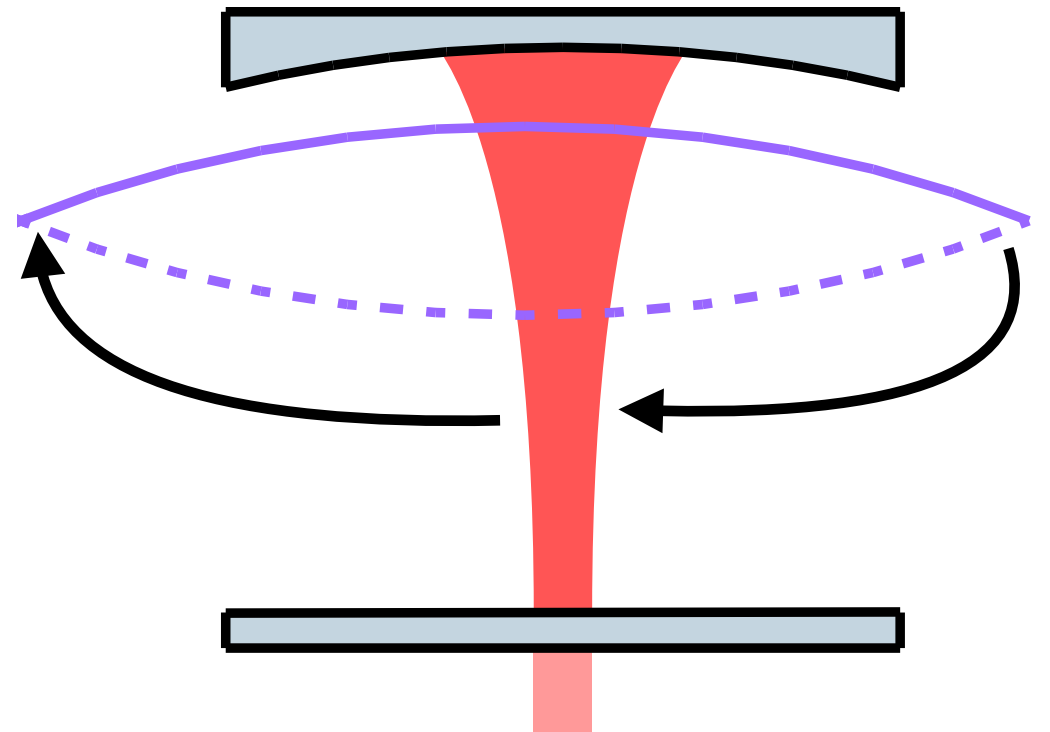
Regal group

Strategy for state conversion

$$H_{\text{int}} = \hbar g_0 a_{\text{mw}}^\dagger a_{\text{mech}} + \text{h.c.}$$

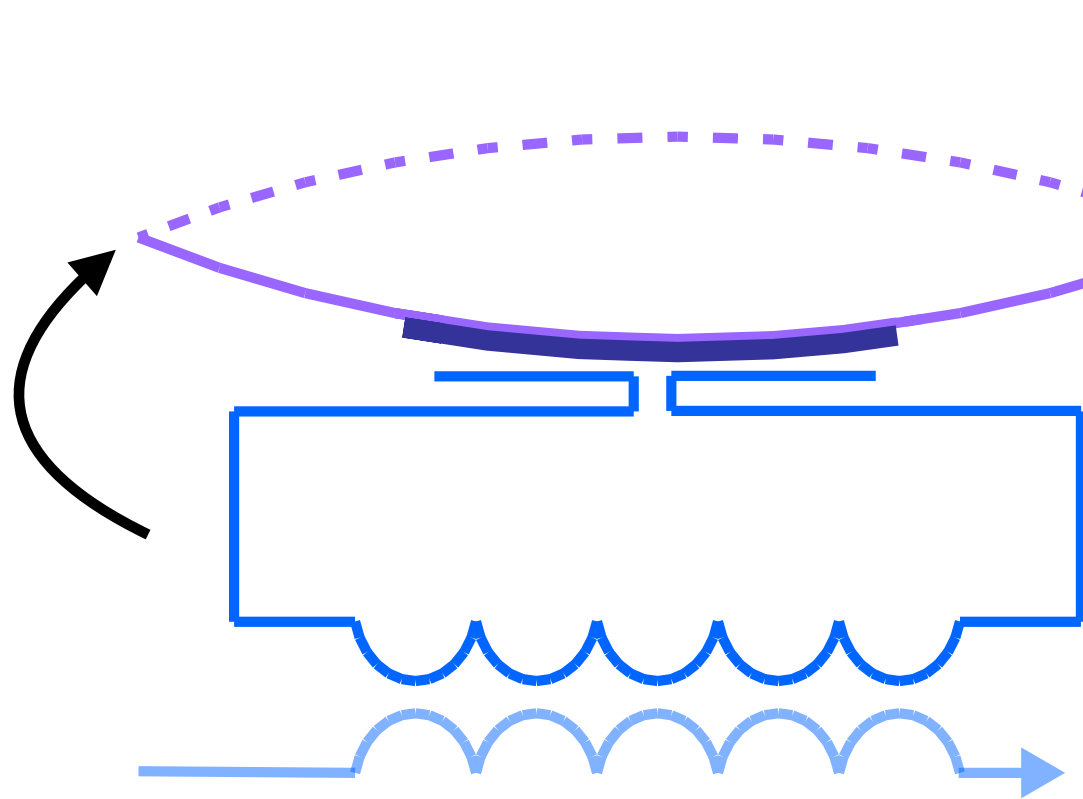


$$H_{\text{int}} = \hbar g_0 a_{\text{opt}}^\dagger a_{\text{mech}} + \text{h.c.}$$

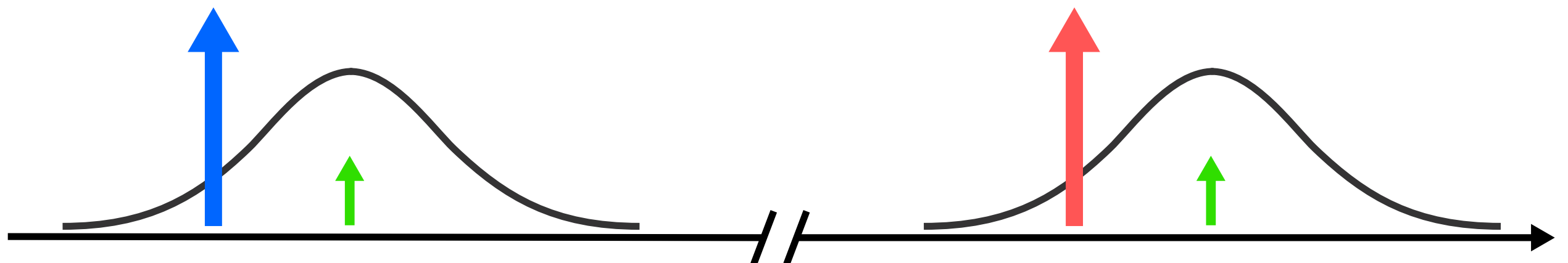
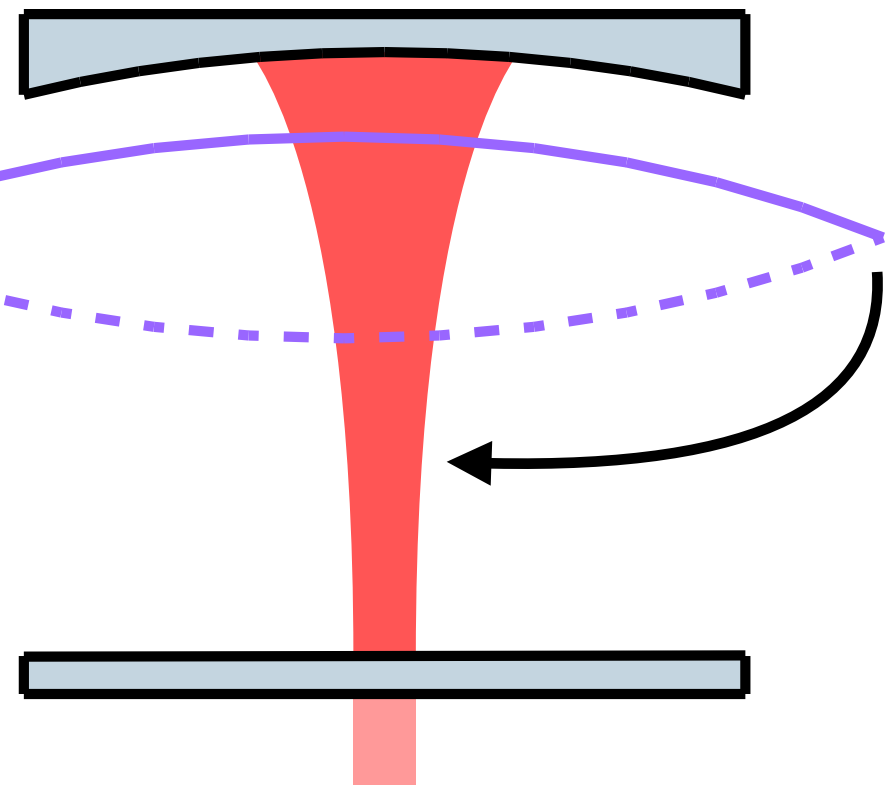


Strategy for state conversion

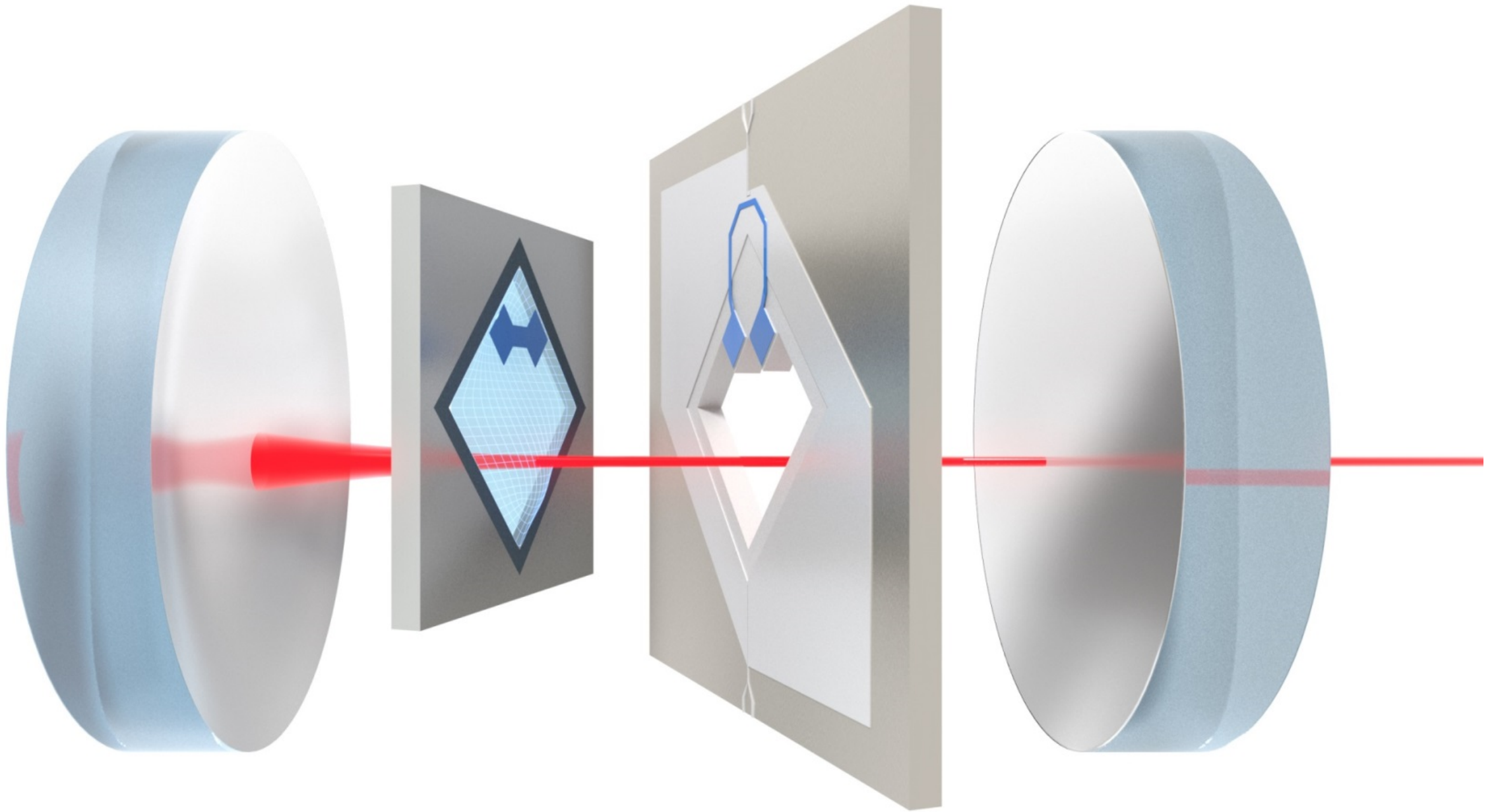
$$H_{\text{int}} = \hbar g_0 a_{\text{mw}}^\dagger a_{\text{mech}} + \text{h.c.}$$



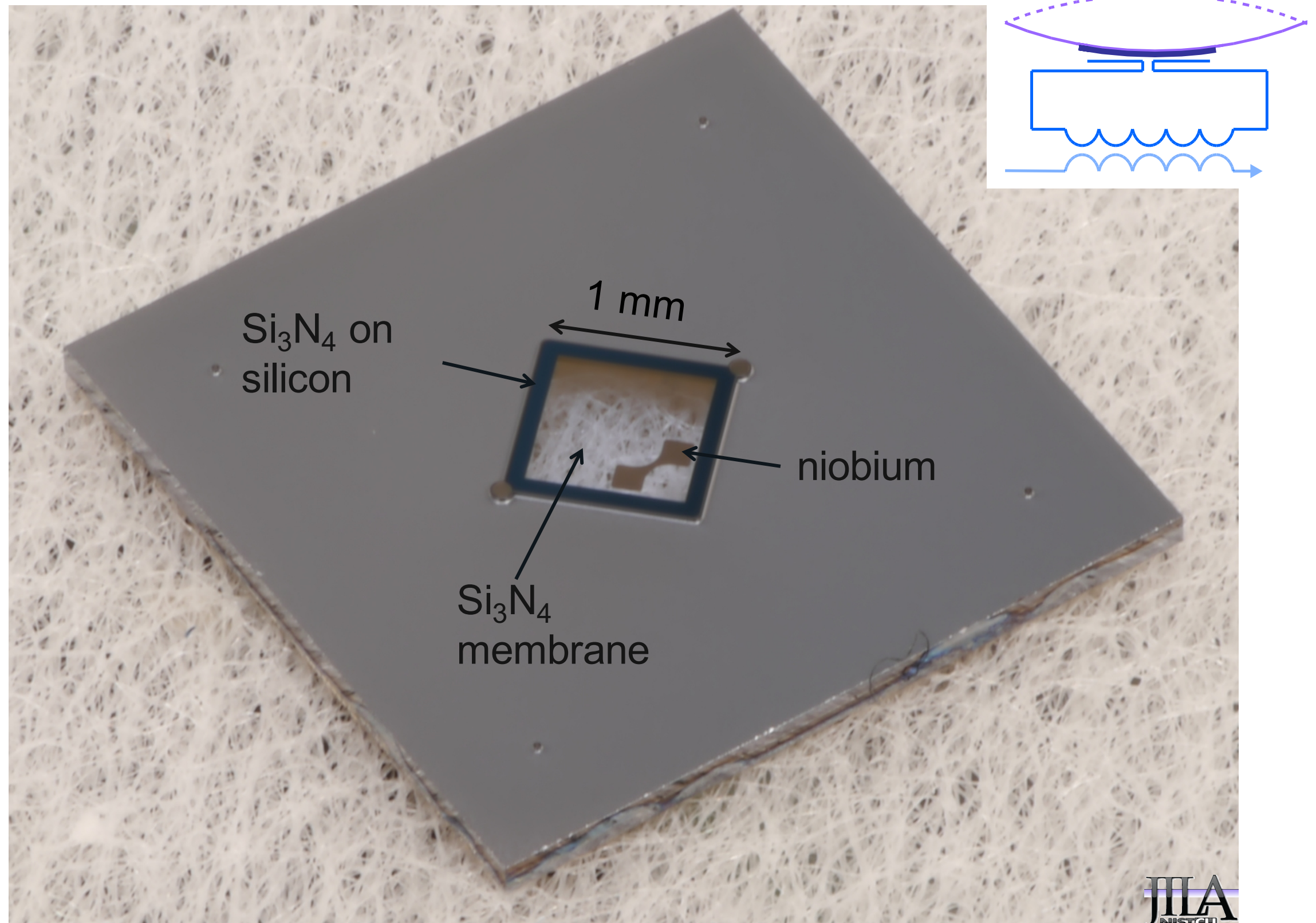
$$H_{\text{int}} = \hbar g_0 a_{\text{opt}}^\dagger a_{\text{mech}} + \text{h.c.}$$



Flip chip in an optical cavity



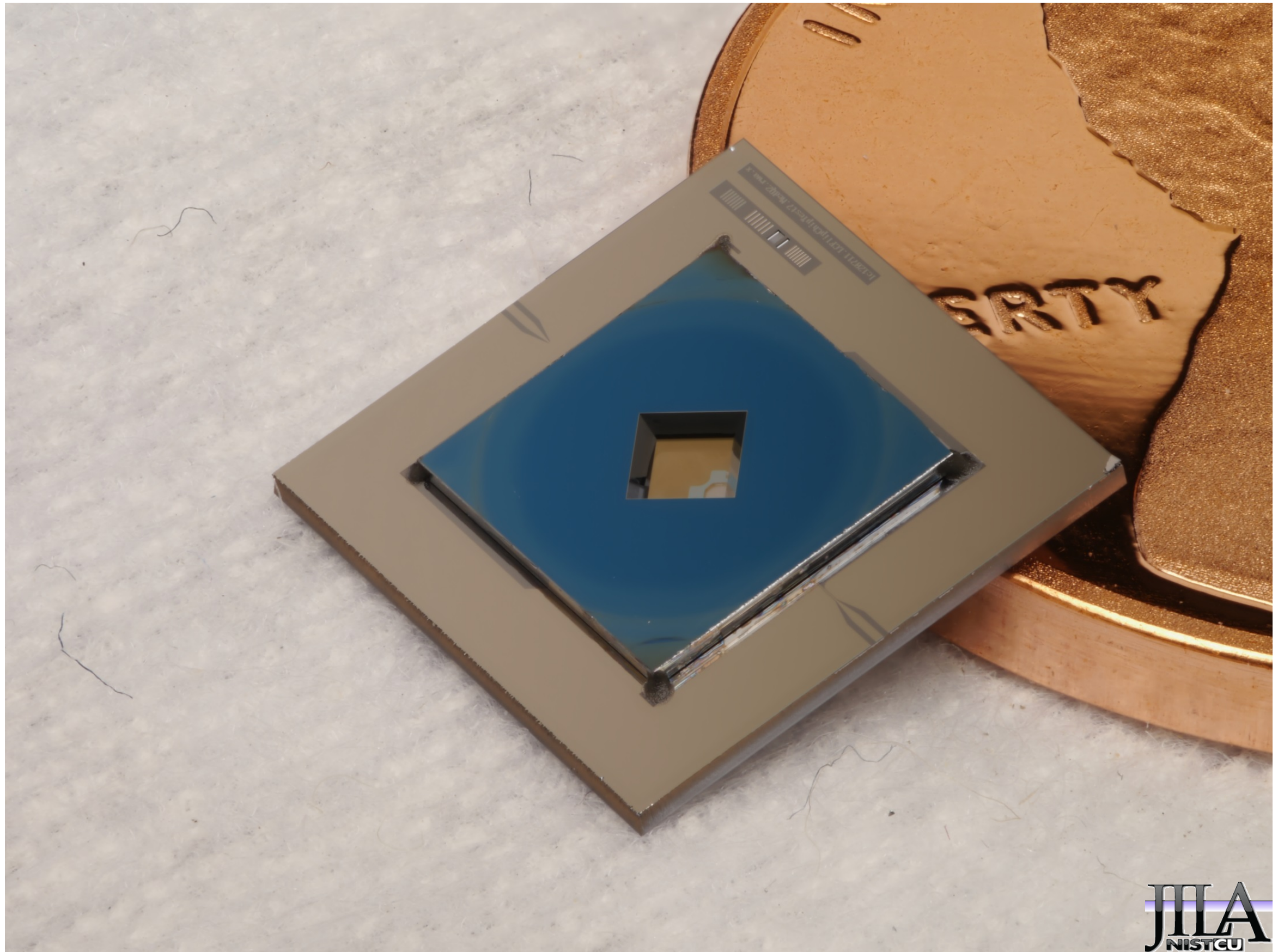
Top chip layout



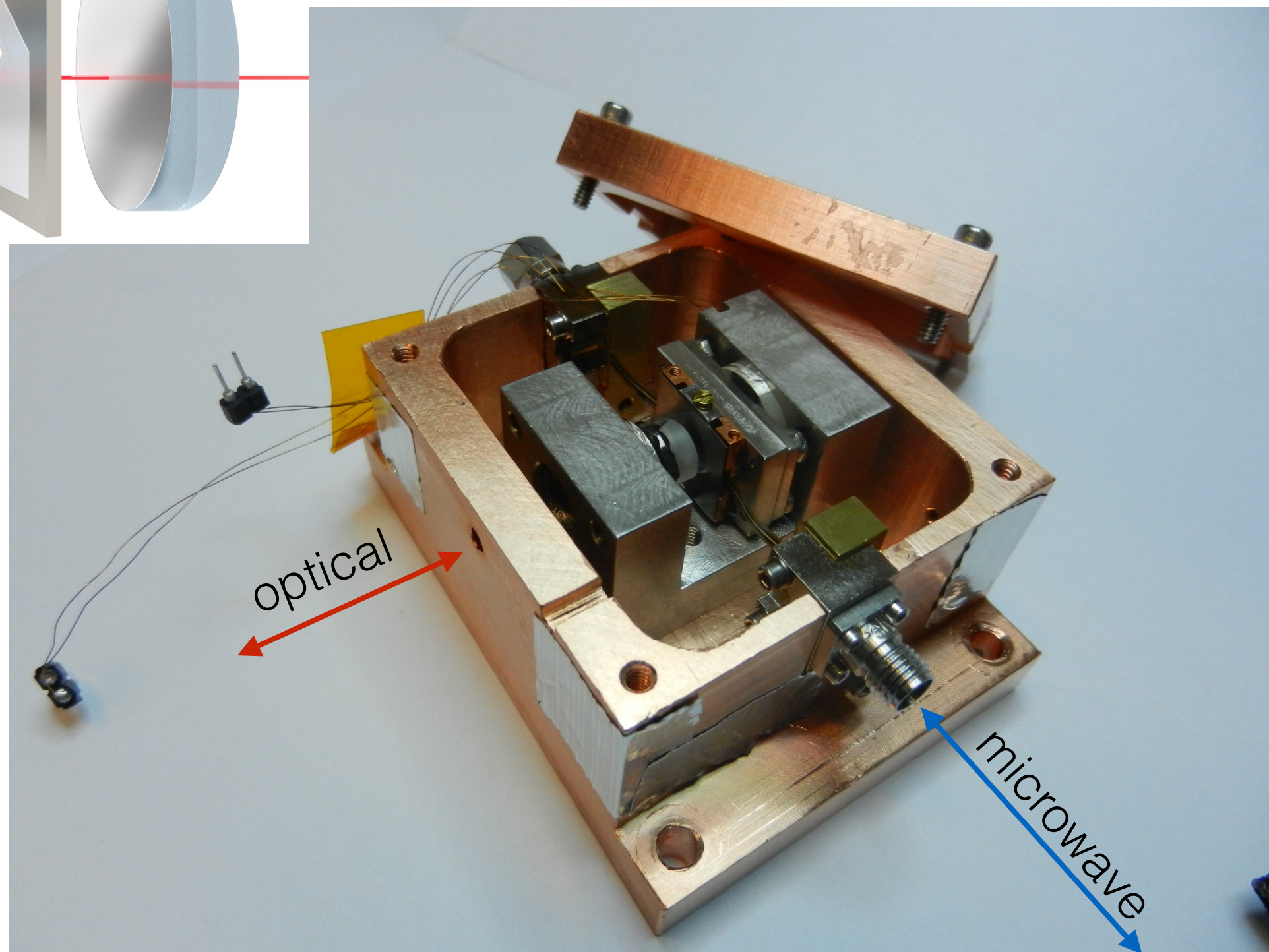
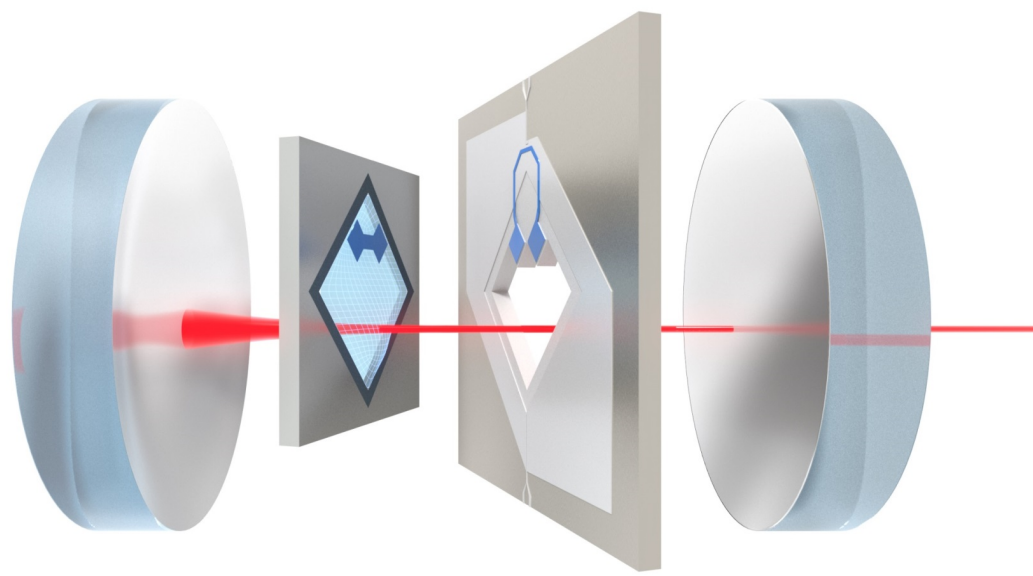
Bottom chip layout



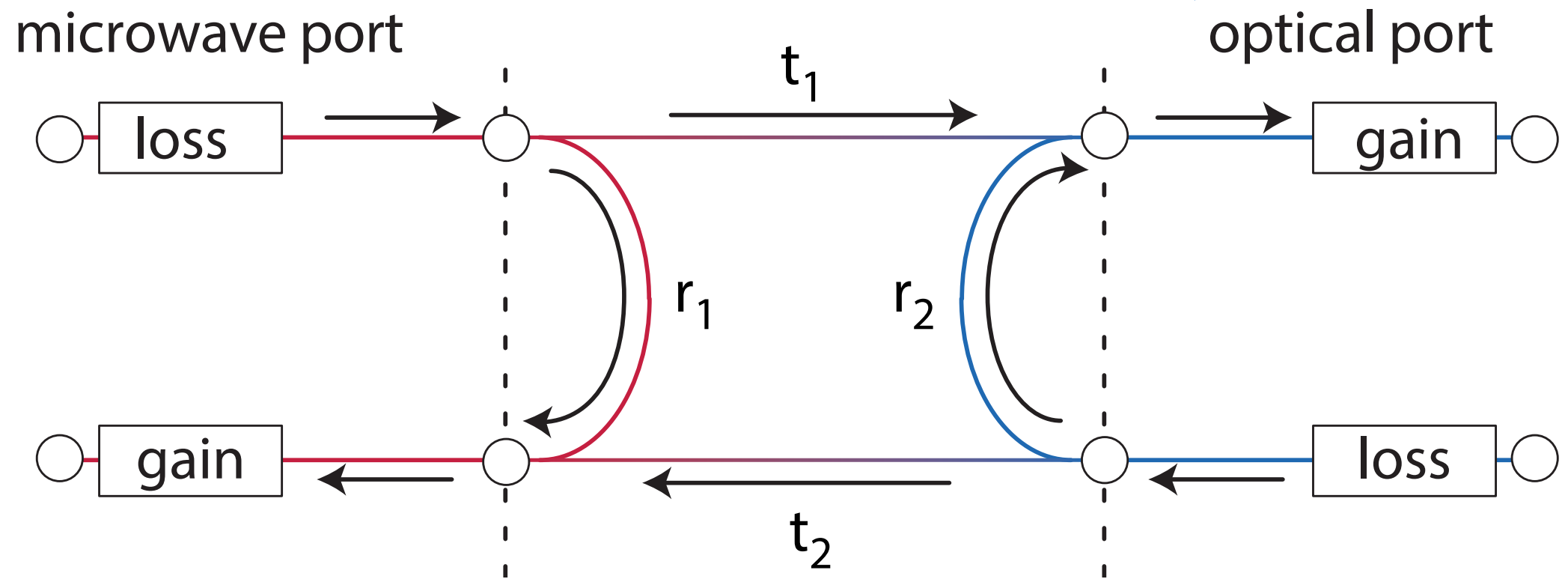
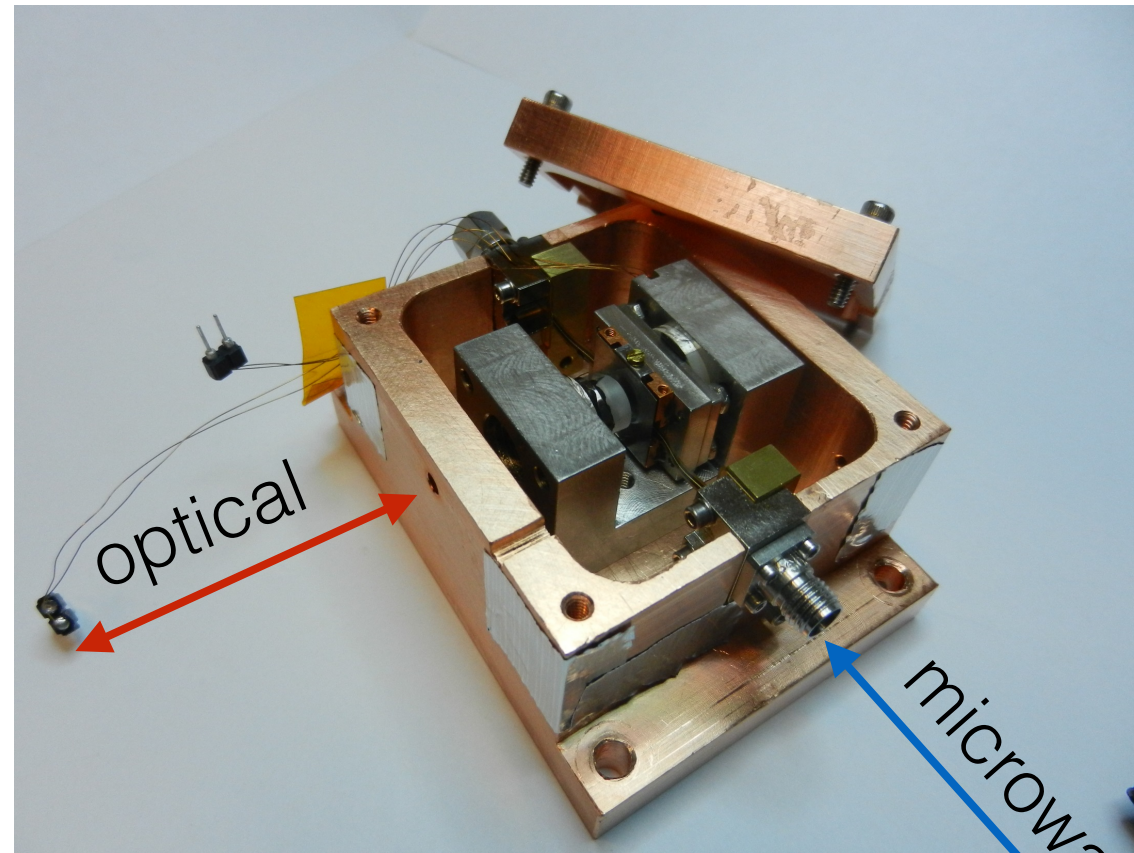
Assembled flip-chip



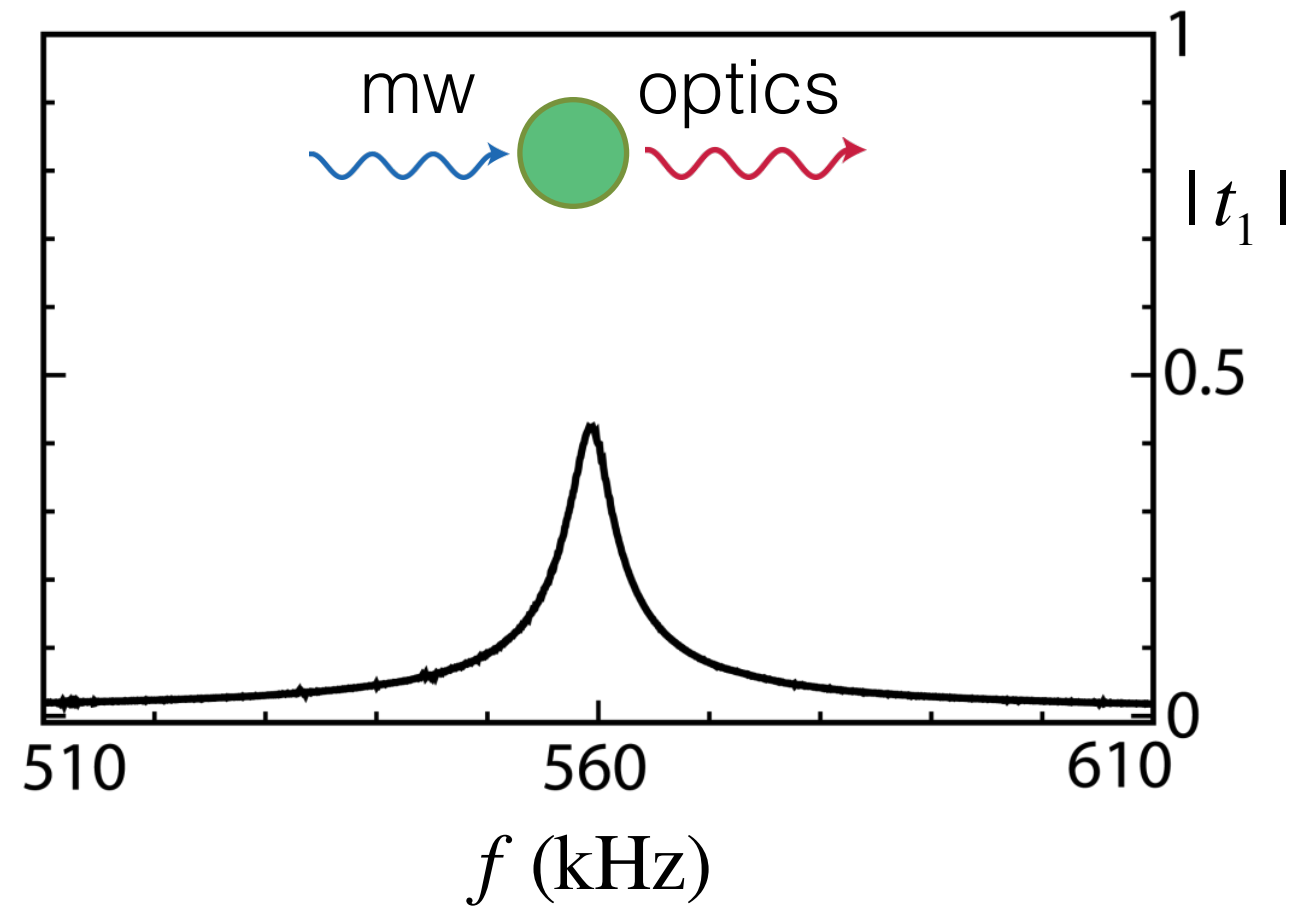
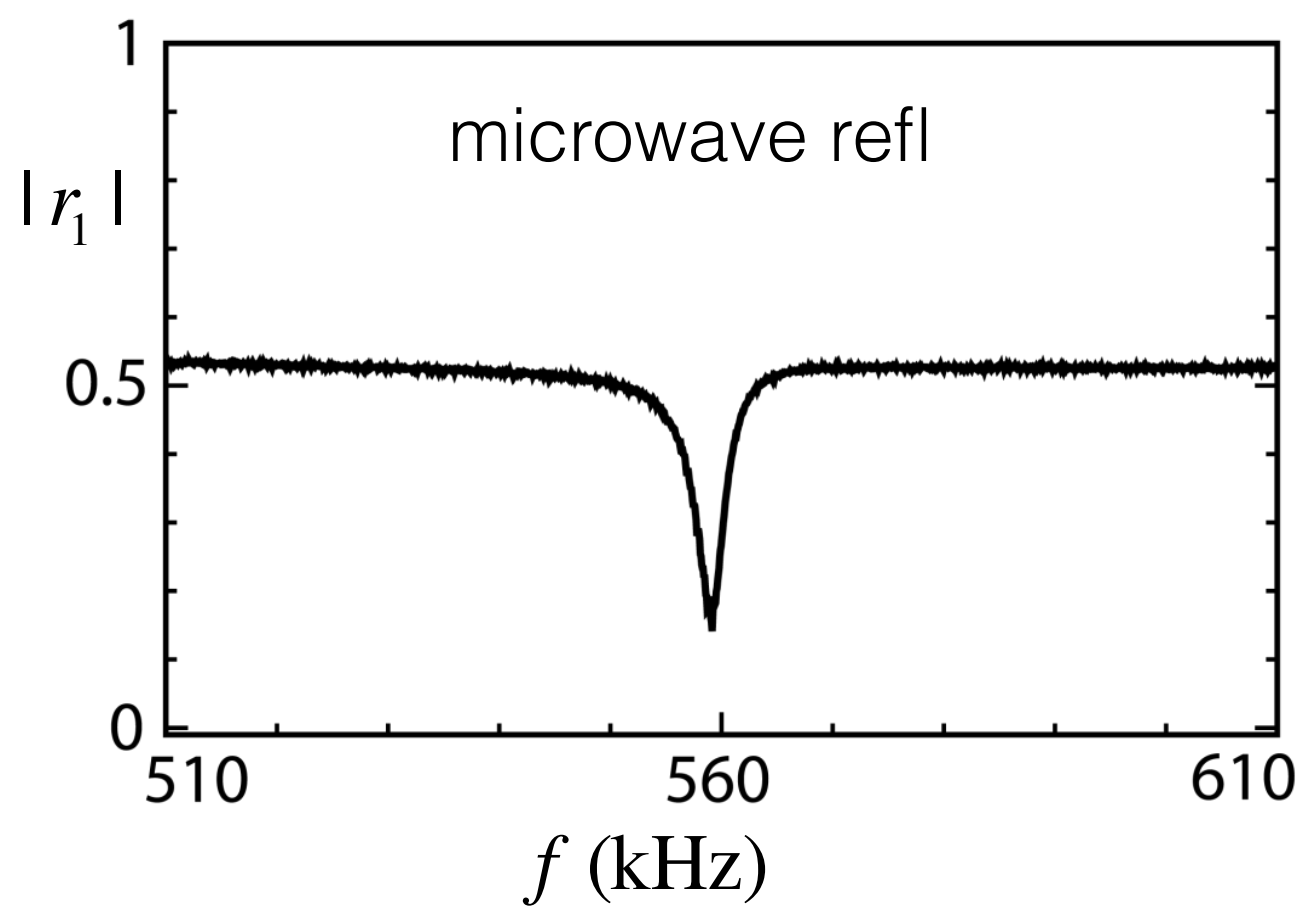
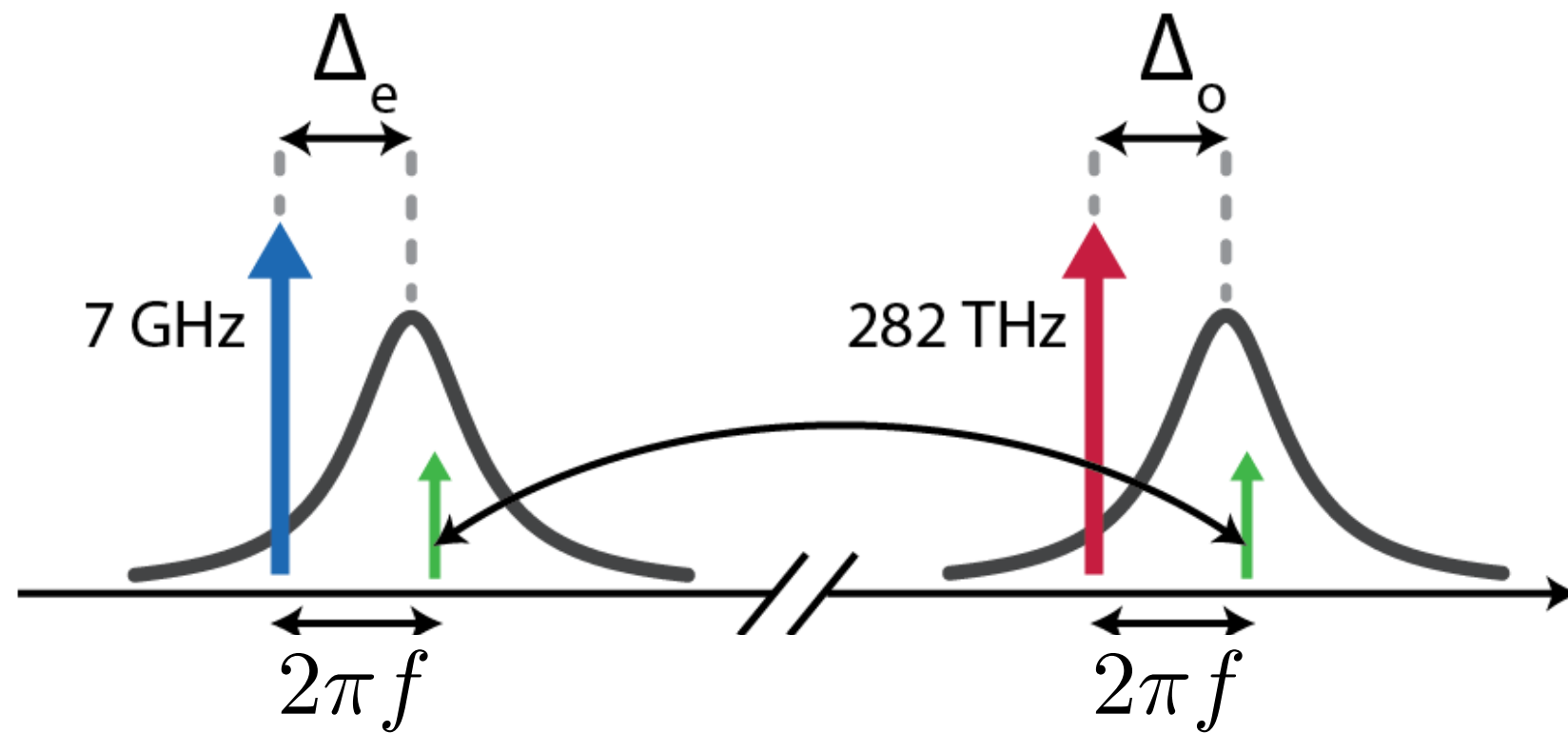
Microwave-mechanical-optical setup



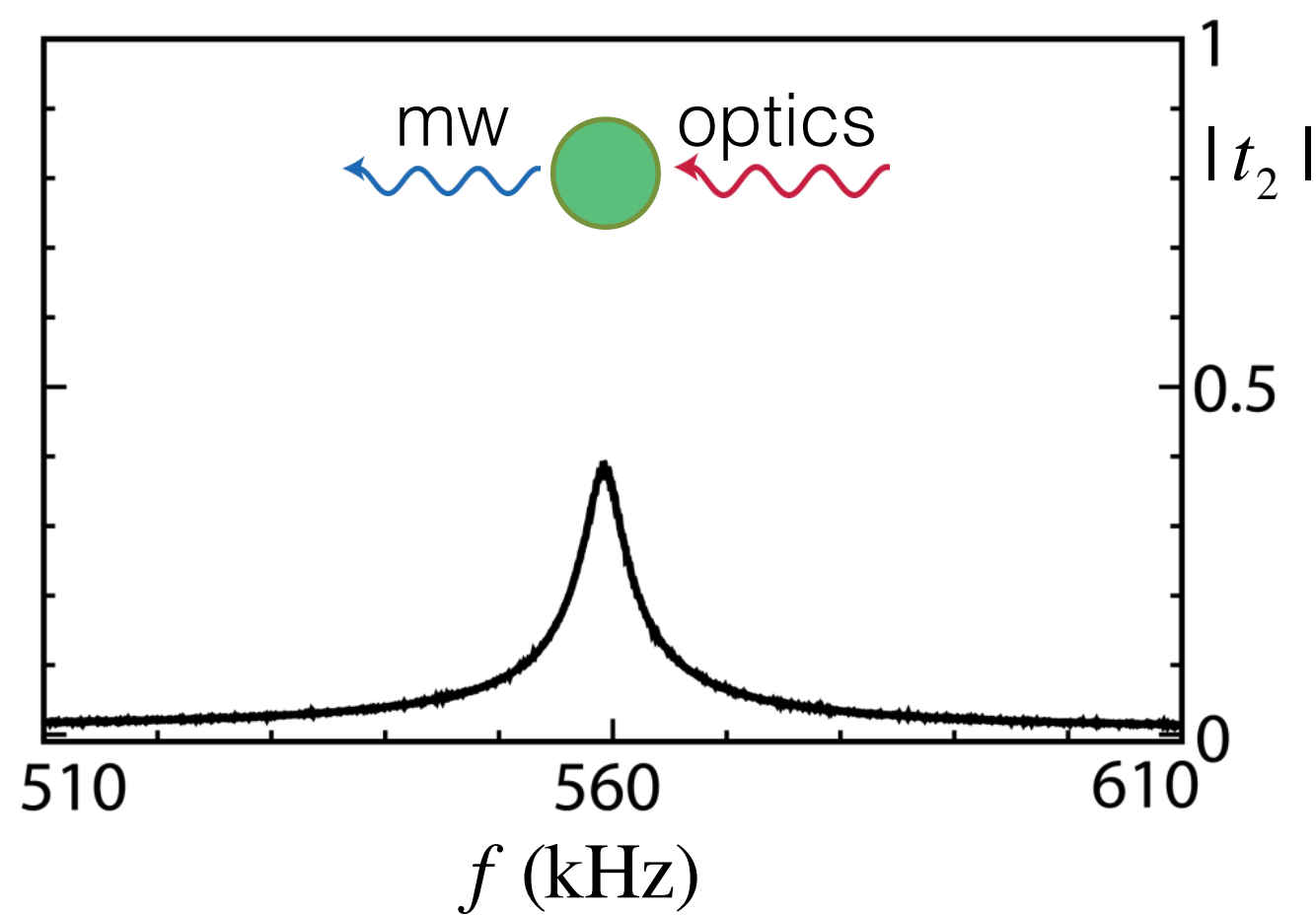
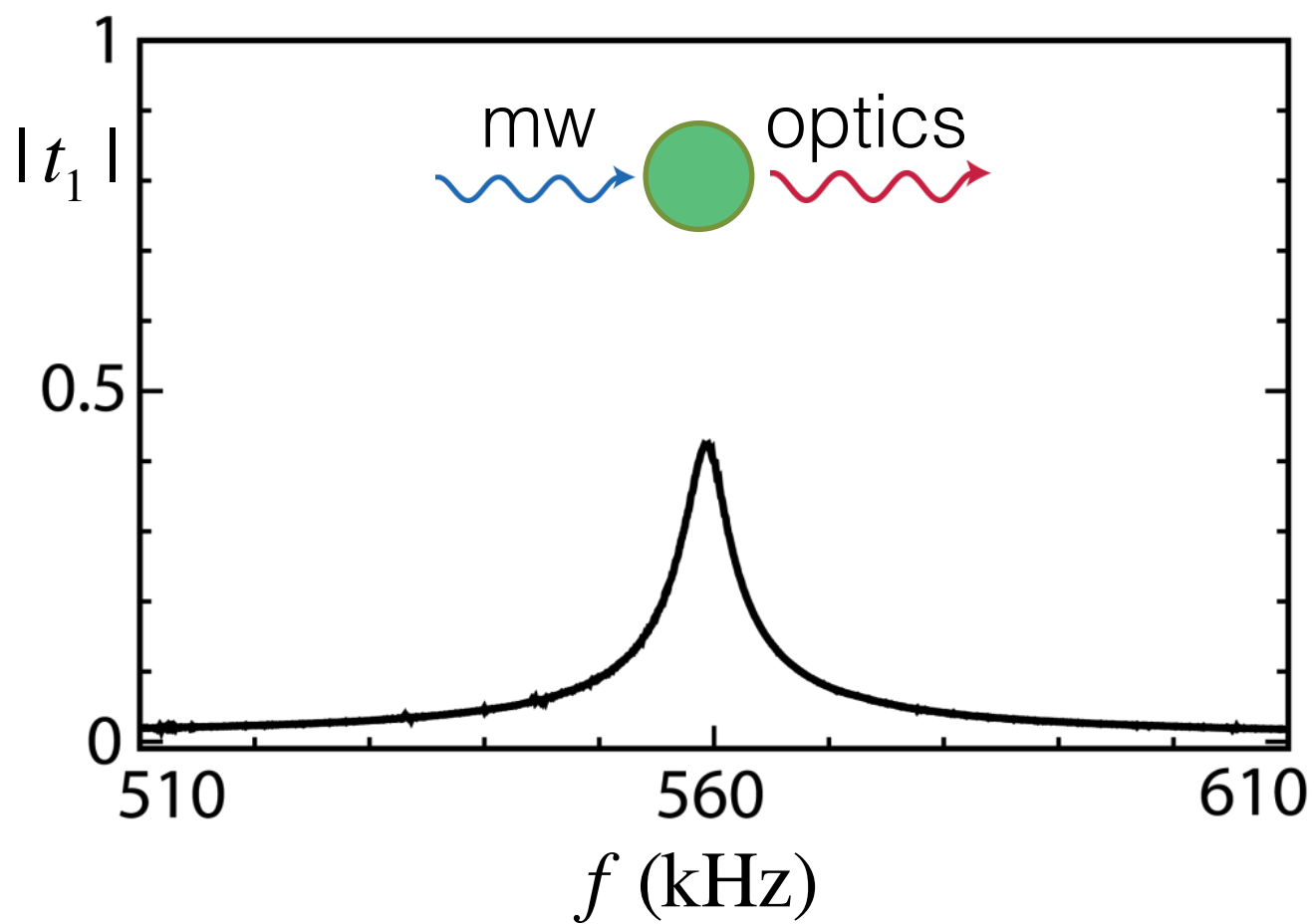
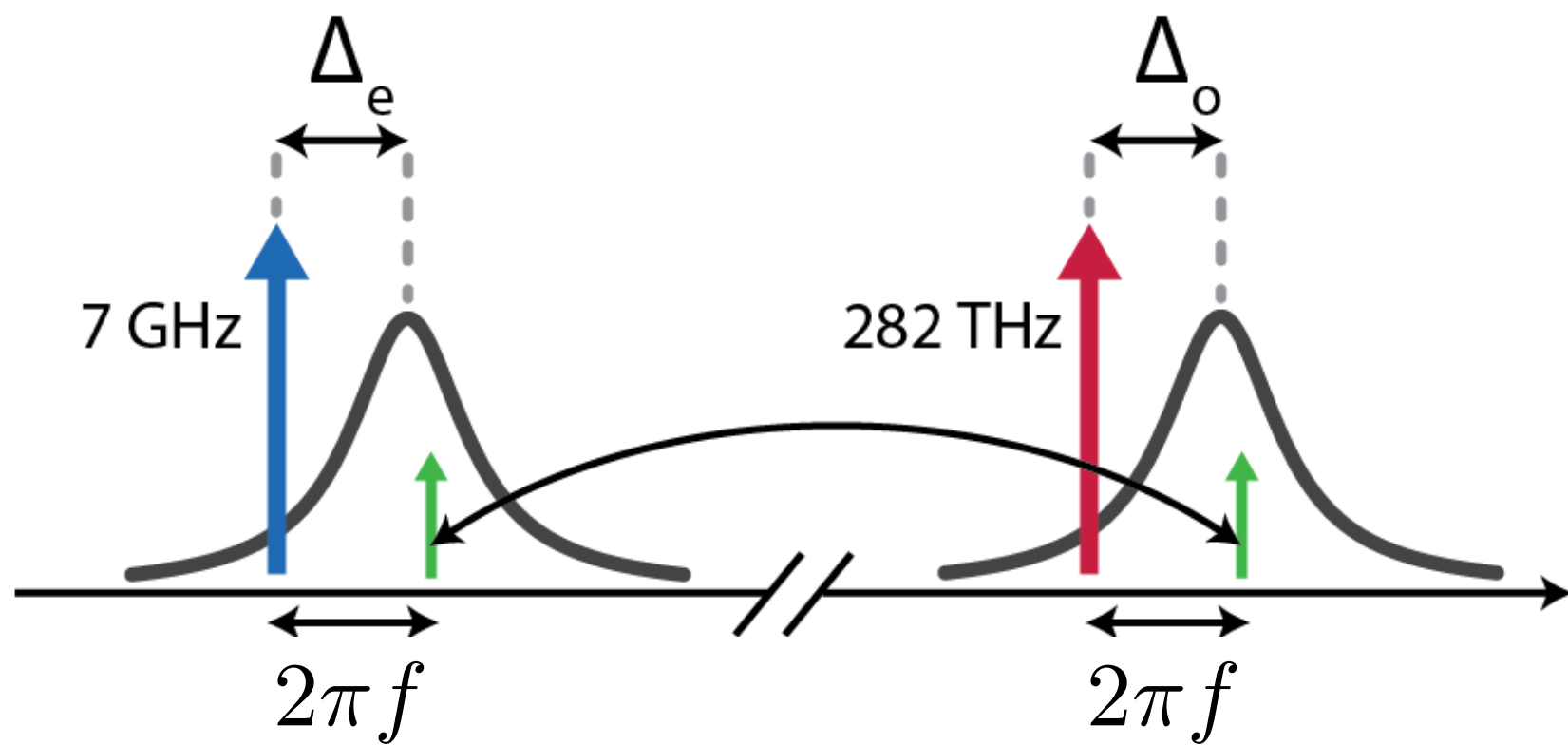
Classical network analysis



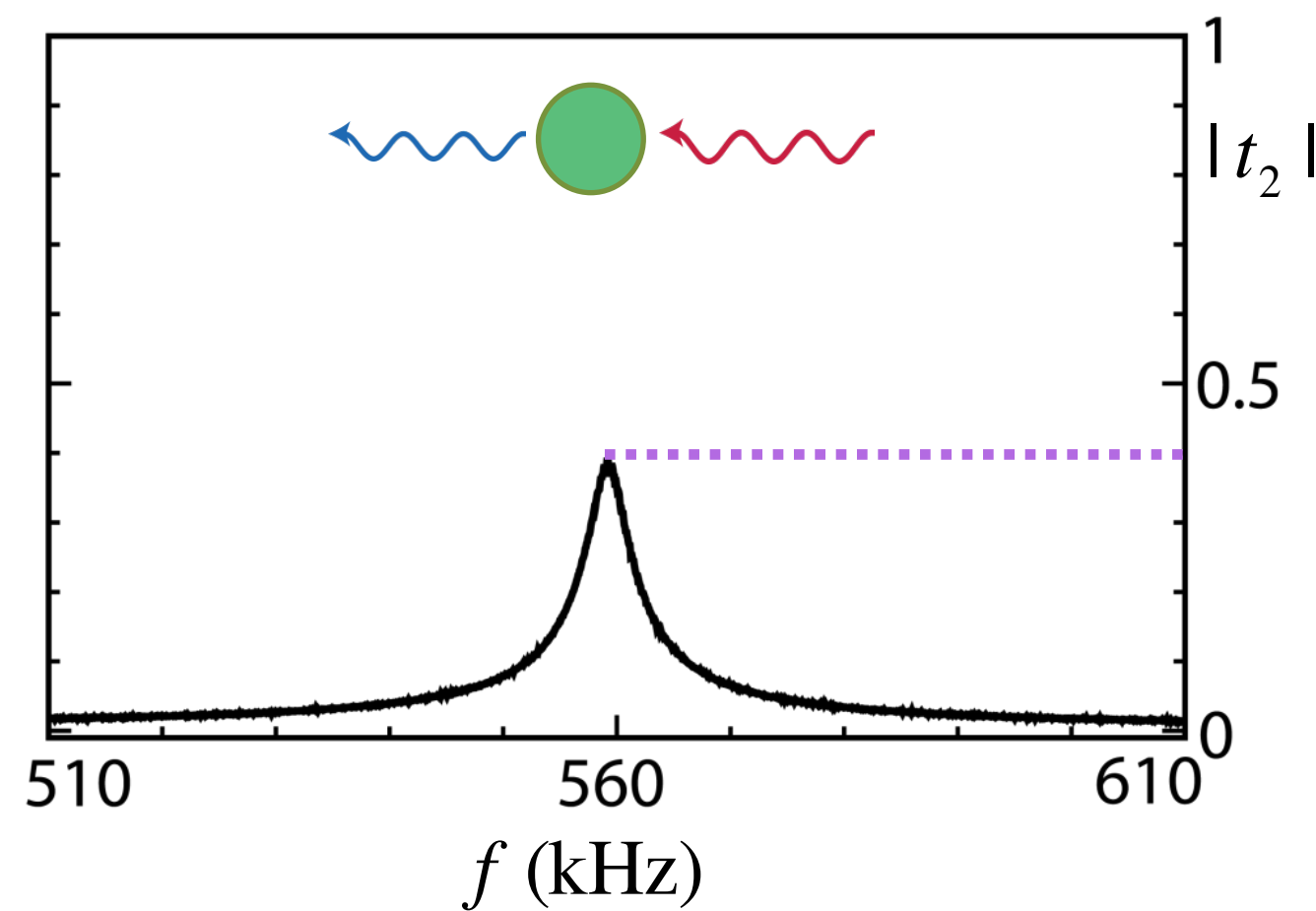
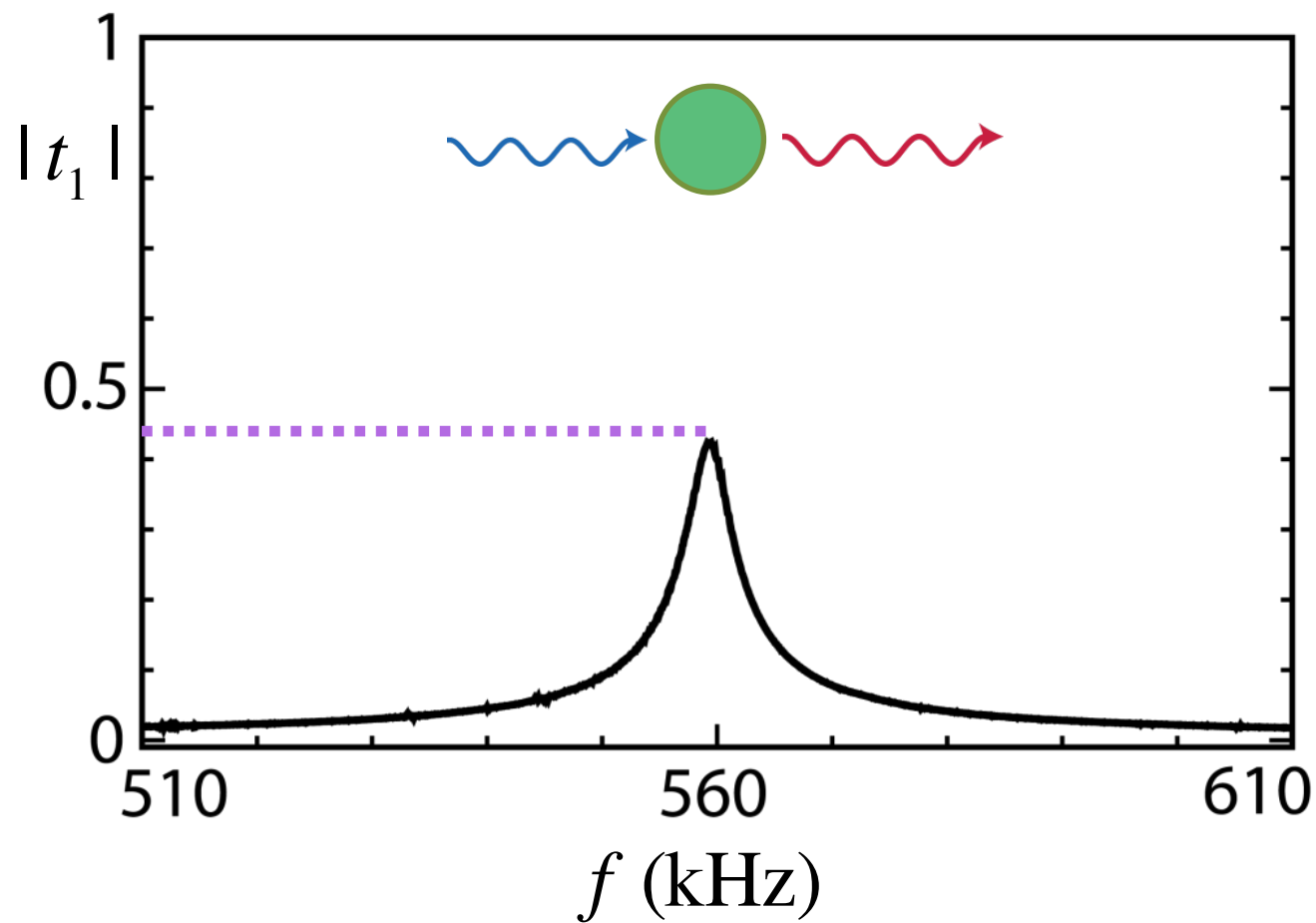
Microwave to optical conversion



Bidirectional conversion



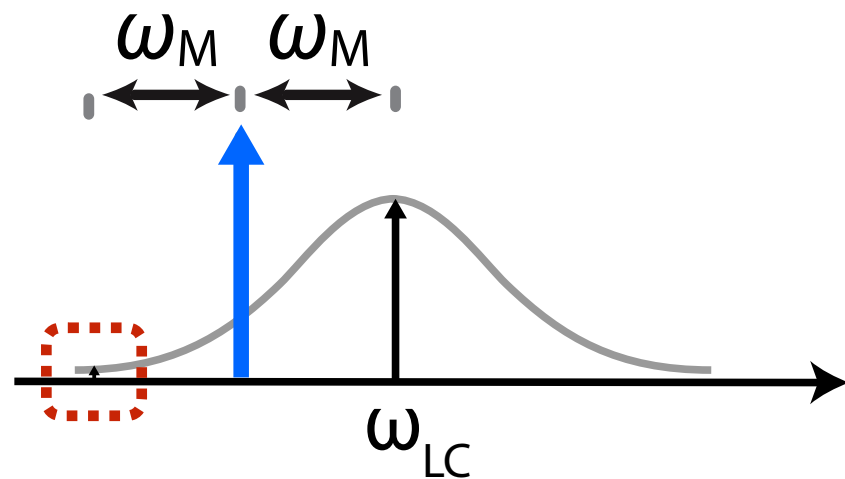
Transfer efficiency



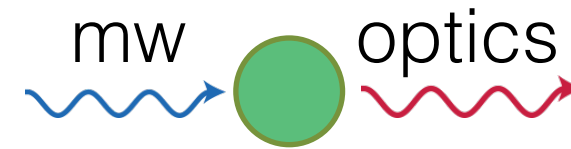
apparent efficiency: $|t_1 t_2| = 0.18$

total gain:
$$\left[1 + \left(\frac{\kappa_e}{4\omega_m} \right)^2 \right] \times \left[1 + \left(\frac{\kappa_o}{4\omega_m} \right)^2 \right]$$

efficiency:
$$\frac{|t_1 t_2|}{\text{Gain}} = 8\%$$



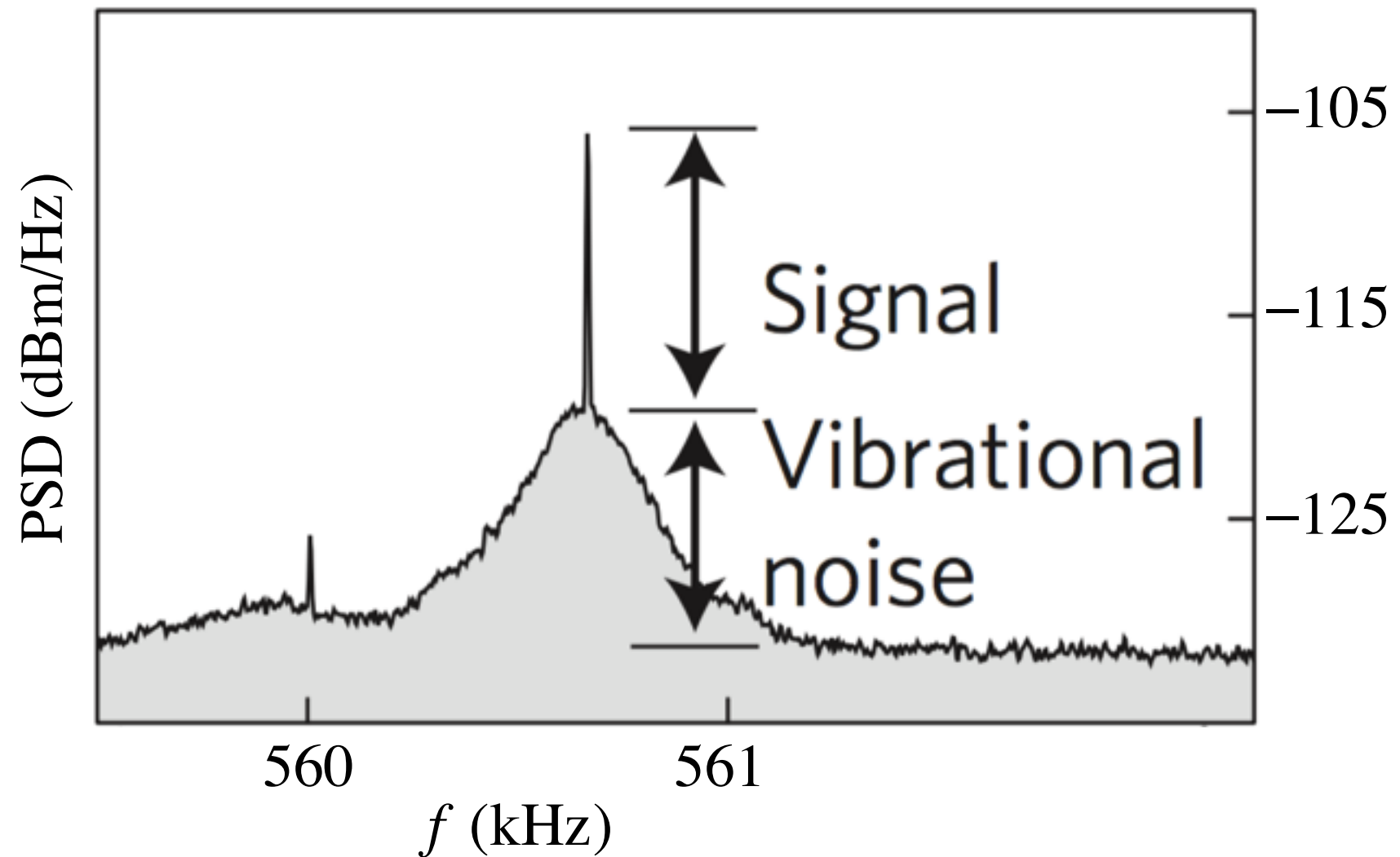
Added noise



best-case added noise:

$$\frac{n_{\text{th}} \gamma_{\text{m}}}{\Gamma_{\text{eo}}} \sim 20 \text{ phonons}$$

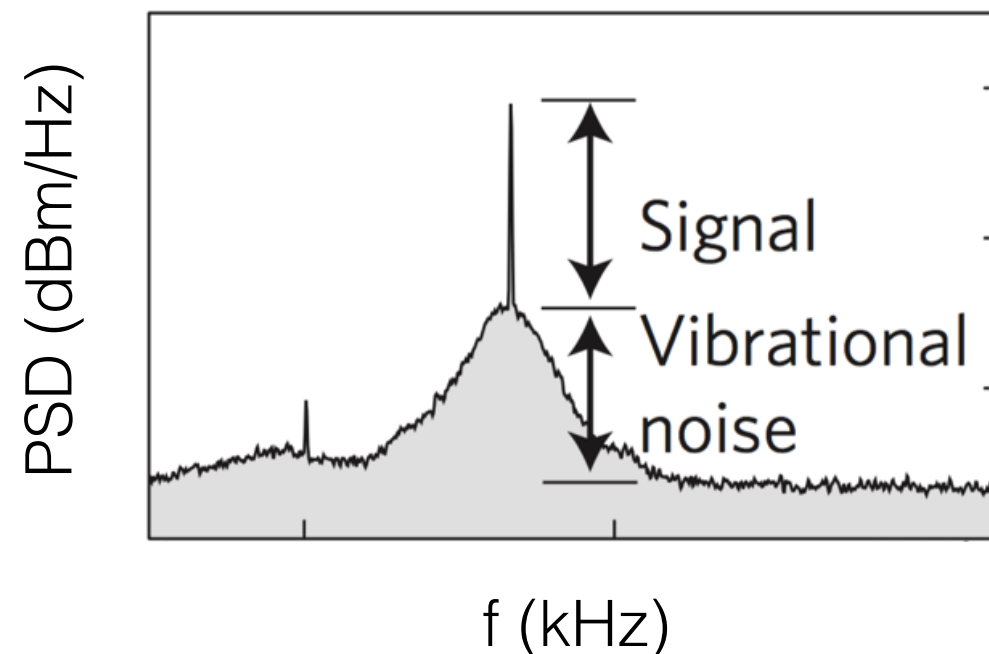
at $T = 4 \text{ K}$



Added noise dominated by mechanics

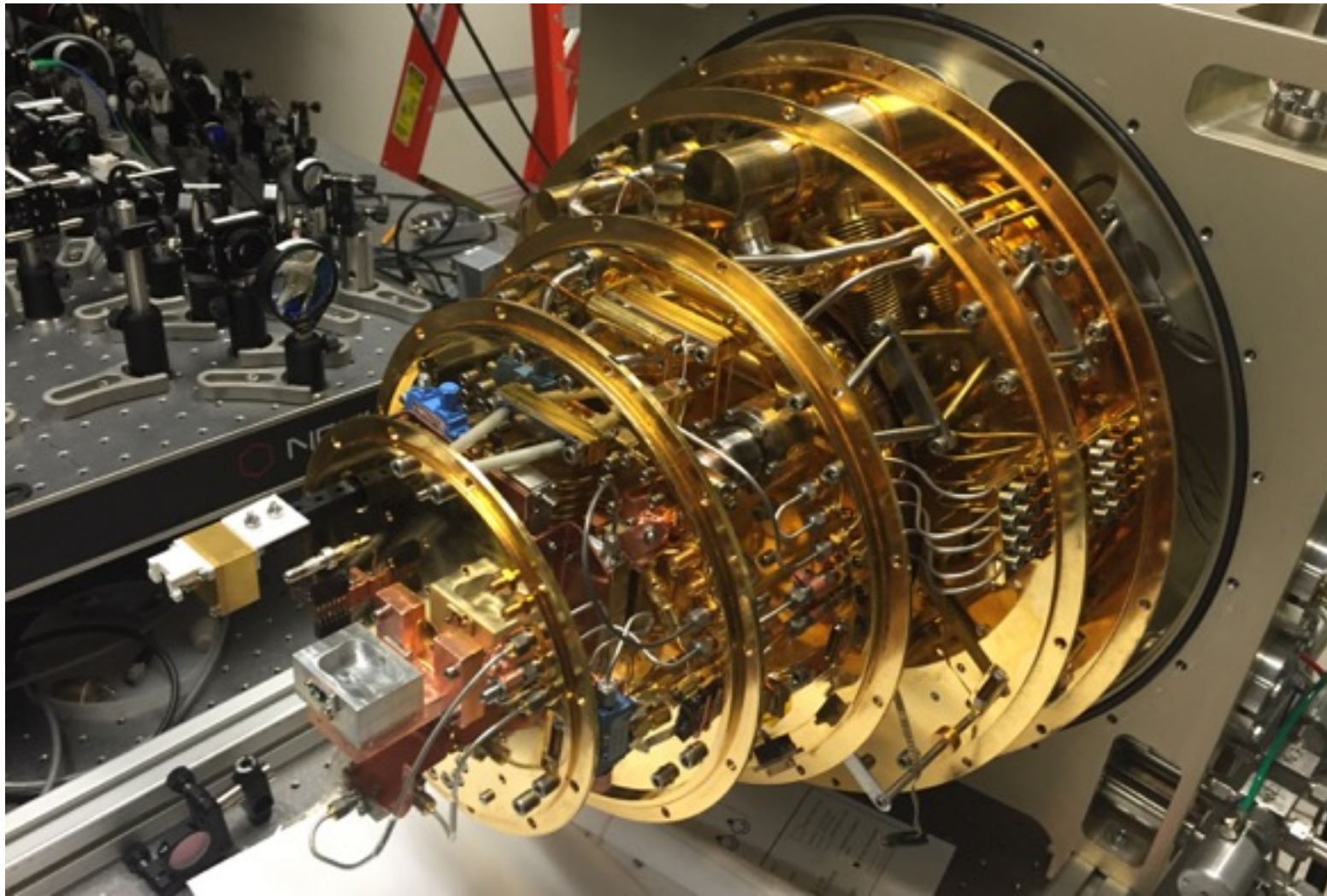
Added noise accounting:

$$\begin{array}{r} \text{Opt. sideband: } 0.5 \\ \text{Microwave sideband: } 0.5 \\ + \quad \text{Mechanics: } 20 \\ \hline \text{Overall: } 21 \text{ quanta} \end{array}$$



To reduce added noise, move to a dilution refrigerator

$$\frac{n_{\text{th}} \gamma_{\text{m}}}{\Gamma_{\text{eo}}} \sim 20 \text{ phonons} \quad \text{at } T = 4 \text{ K} \quad n_{\text{th}} \sim \frac{k T}{\hbar \omega}$$



$$\frac{n_{\text{th}} \gamma_{\text{m}}}{\Gamma_{\text{eo}}} \sim 0.1 \text{ phonons} \quad \text{at } T = 100 \text{ mK}$$

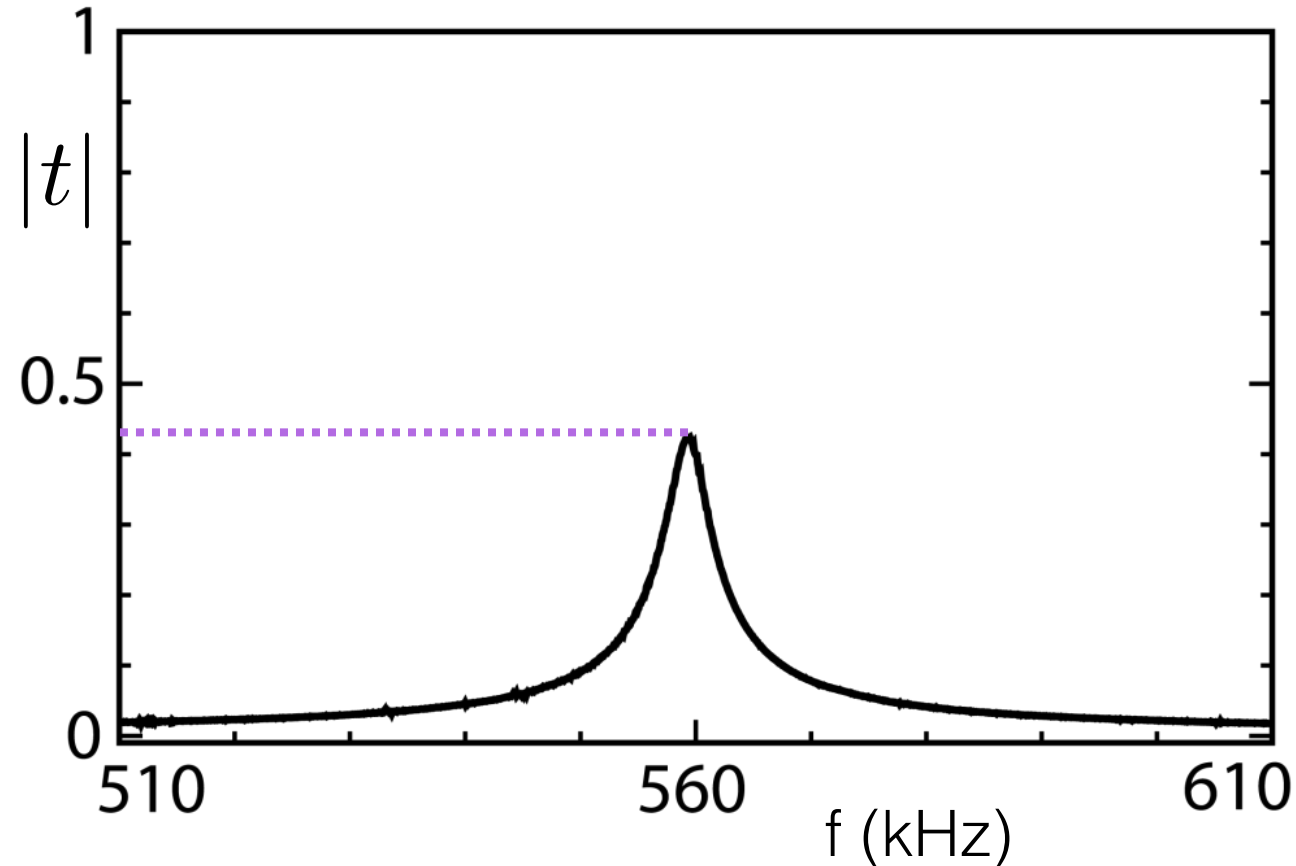
R. W. Peterson et . al. , PRL (2016)

Inefficiency dominated by optical cavity

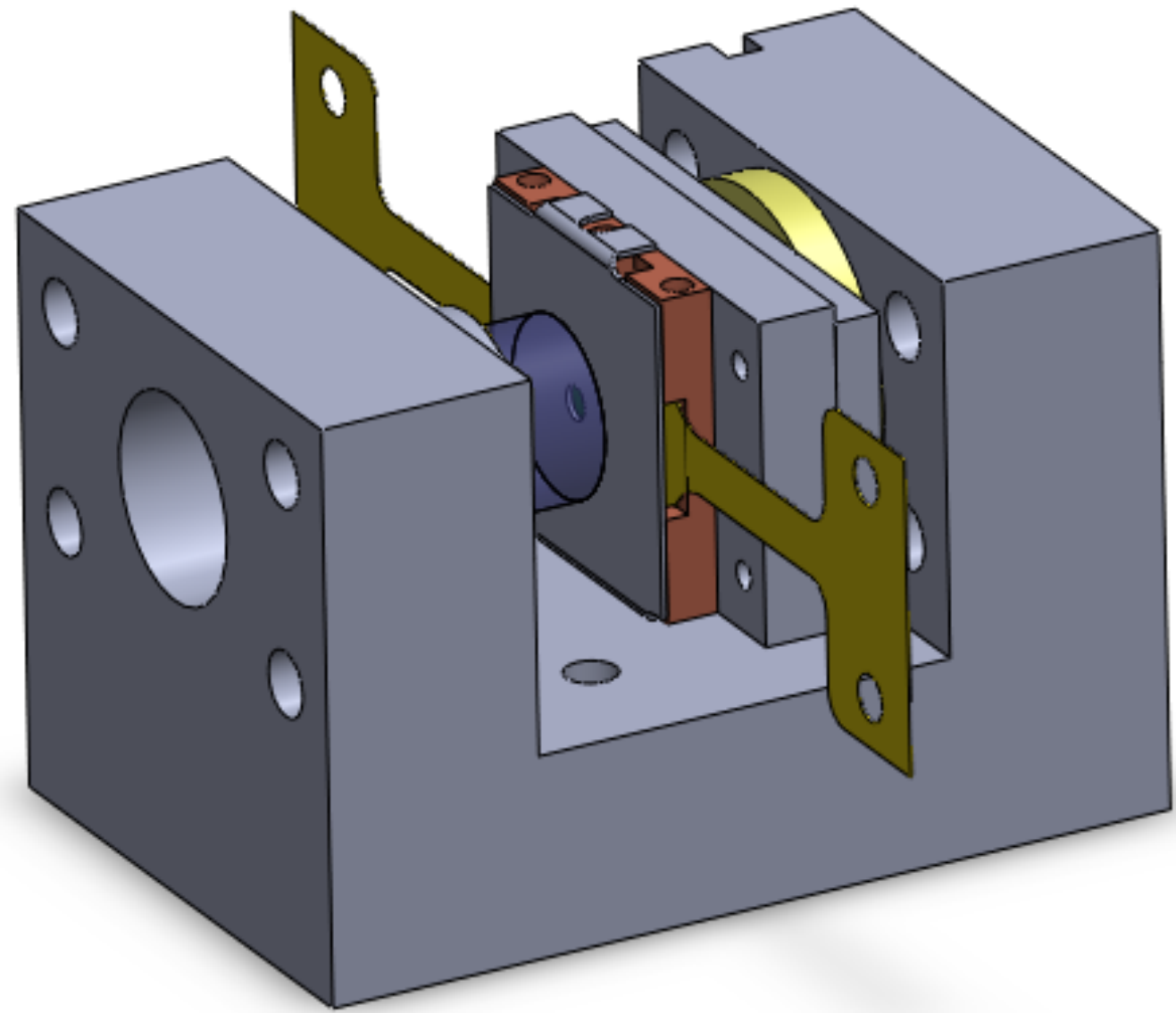
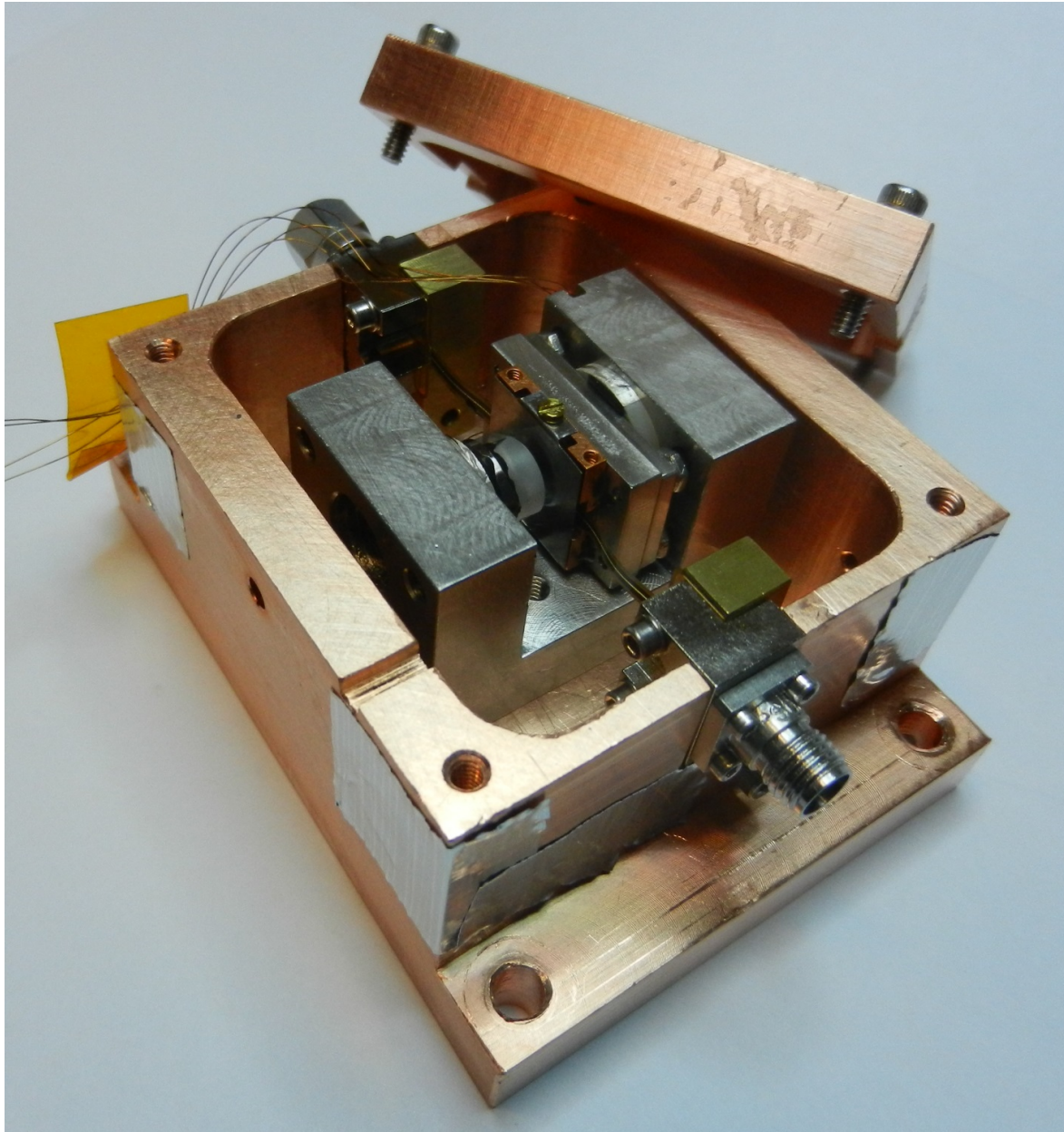
Efficiency accounting:

Optical cavity loss: 0.23
Opt. modematching: 0.5
Microwave loss: 0.76
X Mechanical loss: 0.9998

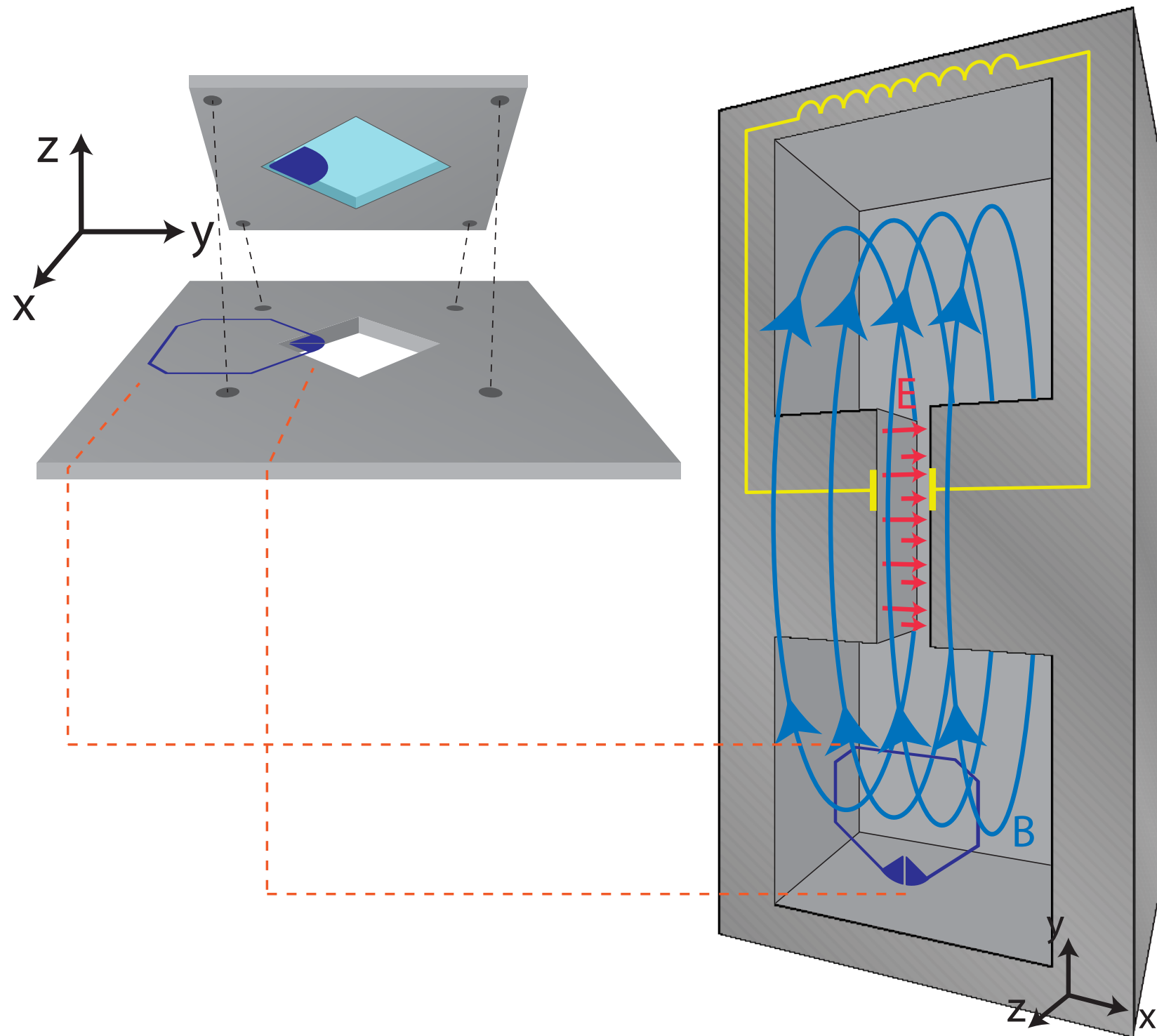
Overall efficiency: 8.7%



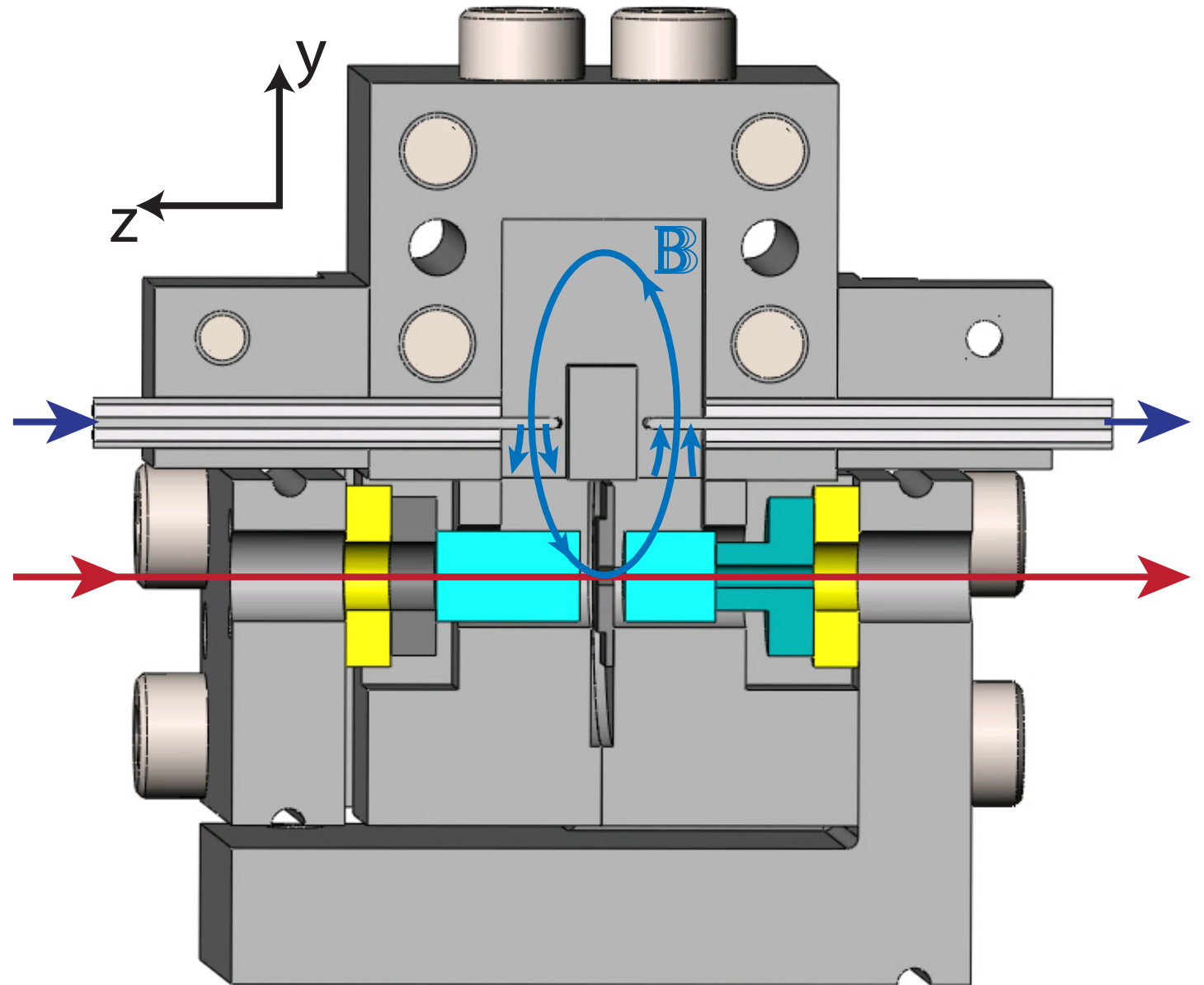
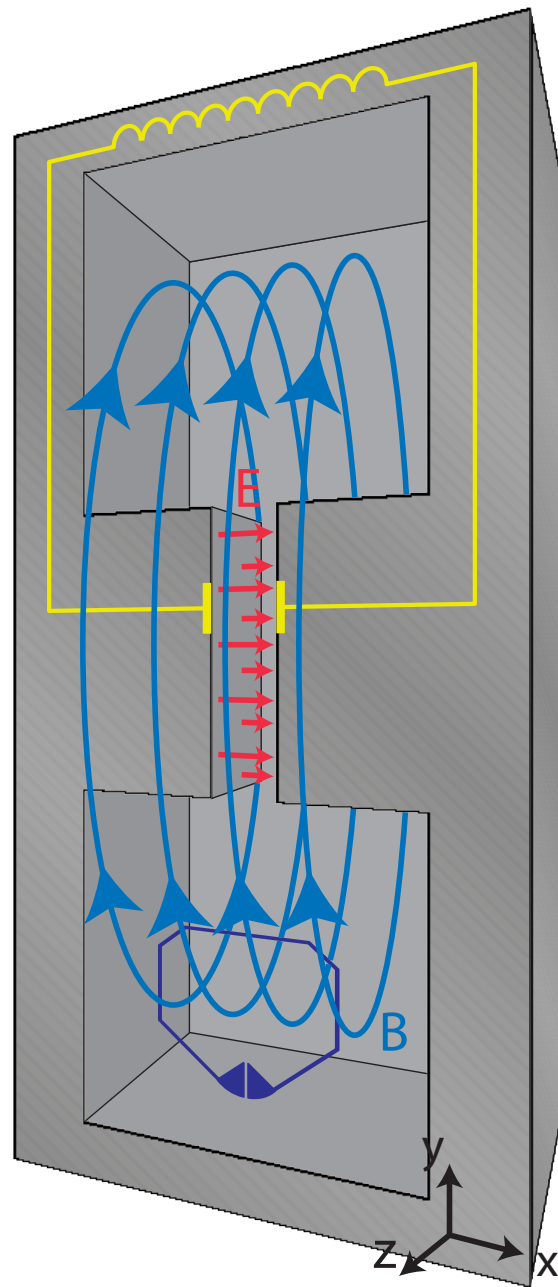
Microwave wiring likely misaligns optical cavity, leading to loss



Wireless approach to microwave coupling

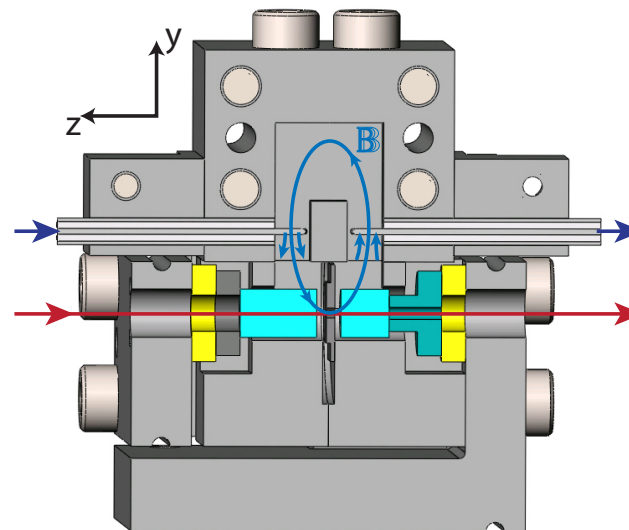
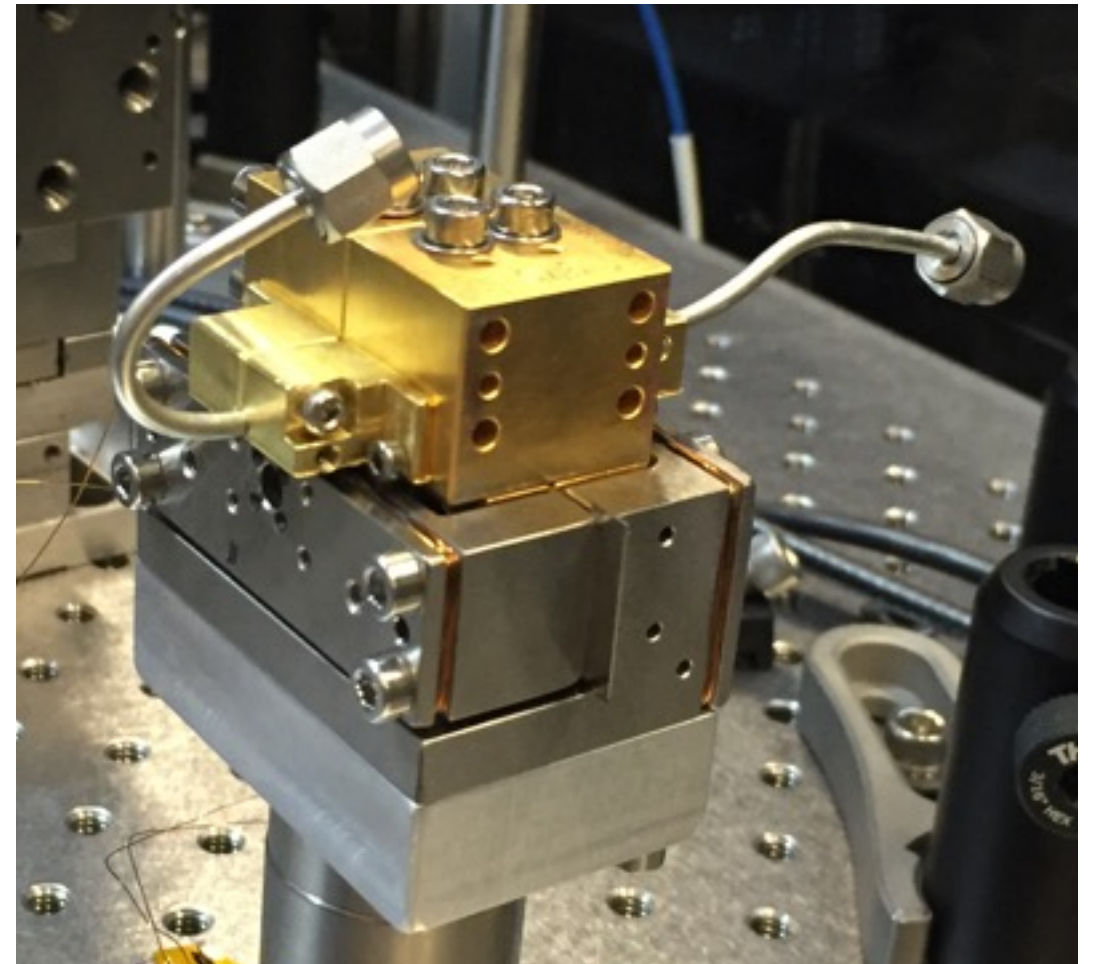
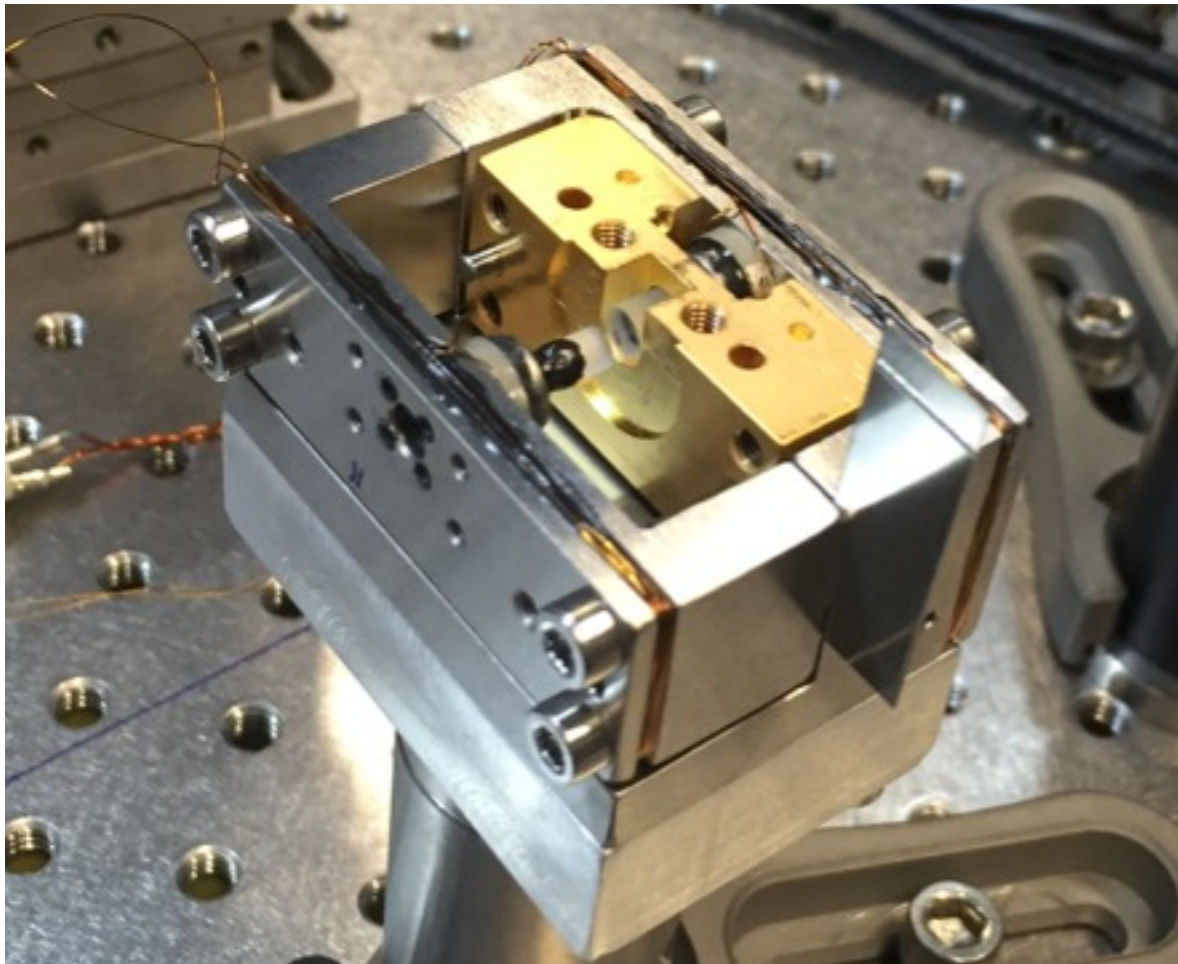


Adding an optical port

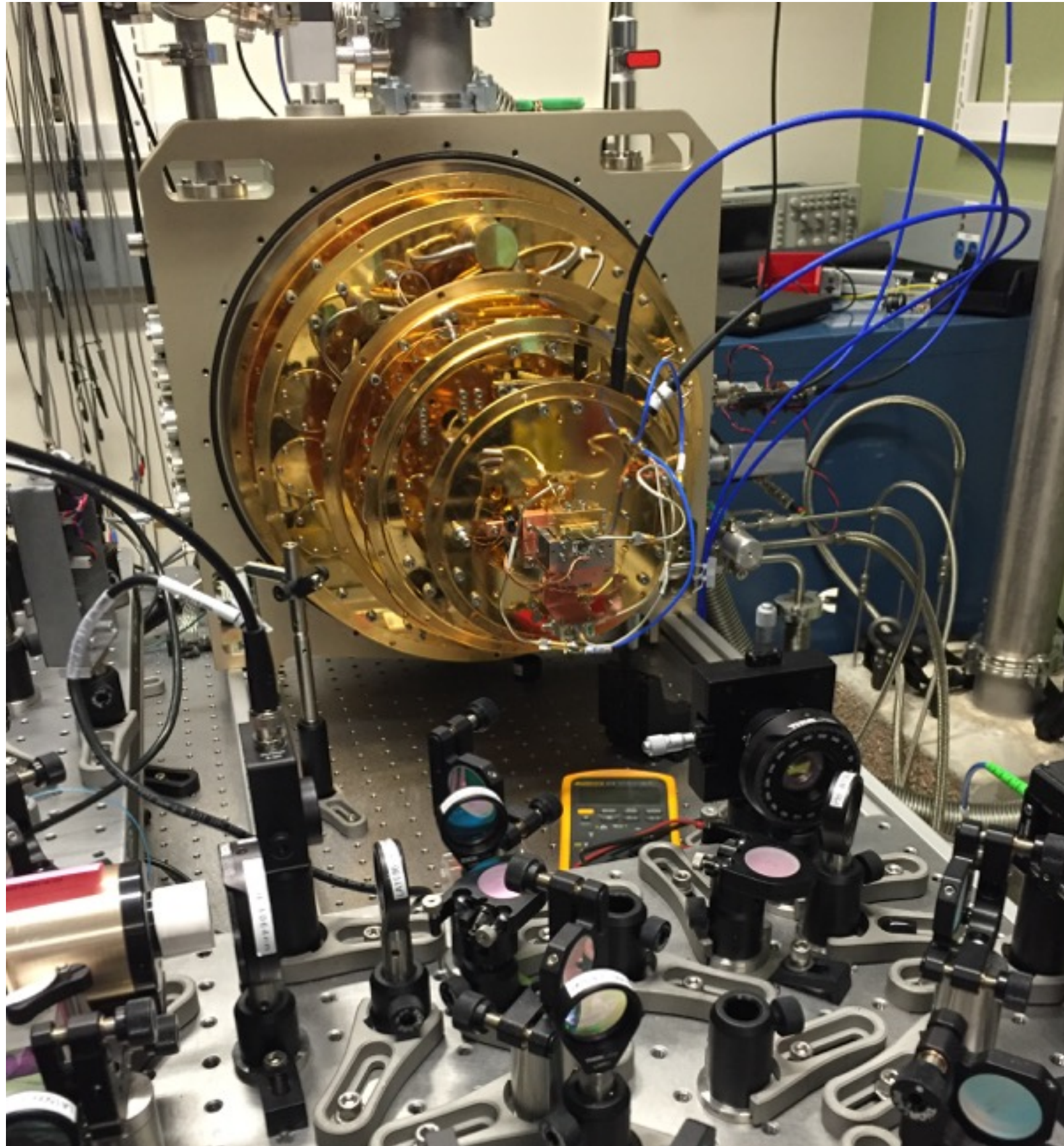


cavity-lc coupling efficiency: 0.9

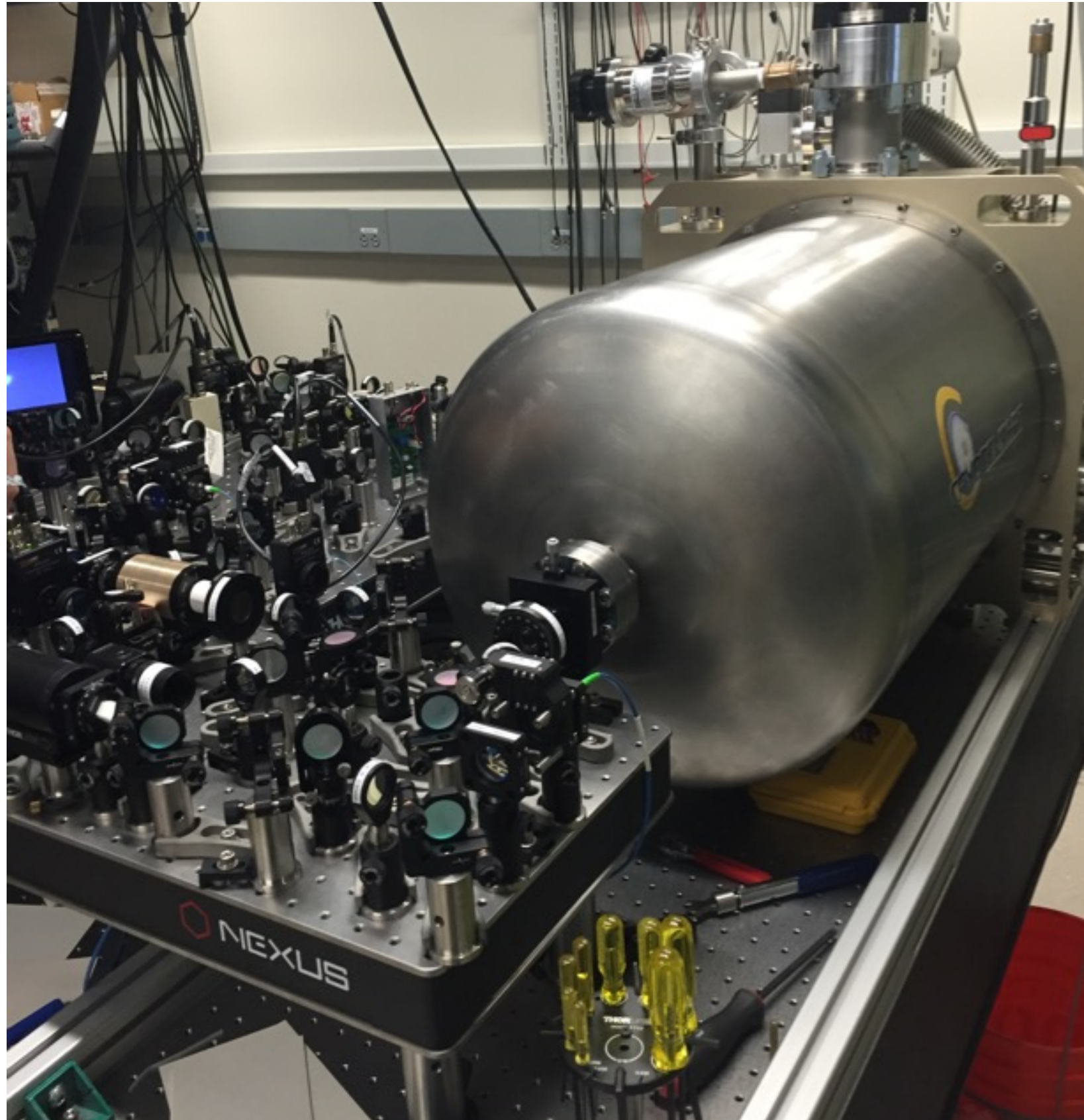
Assembling the converter



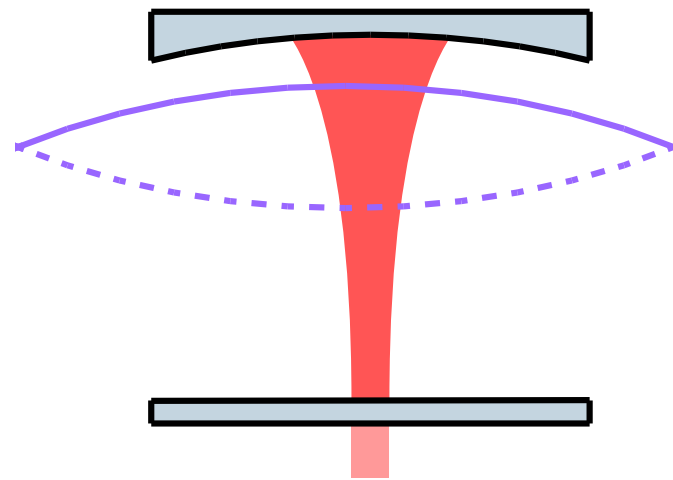
Converter in the cryostat



Cold!



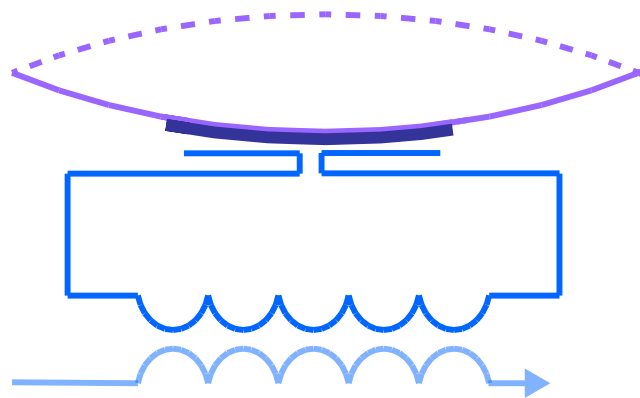
System parameters at 100 mK



optical linewidth: $\kappa_o = 2\pi \text{ 1.8 MHz}$

optical efficiency: $\eta_o = \frac{\kappa_{o,\text{ext}}}{\kappa_o} = 0.7$

optical mode-matching: $\epsilon = ?$

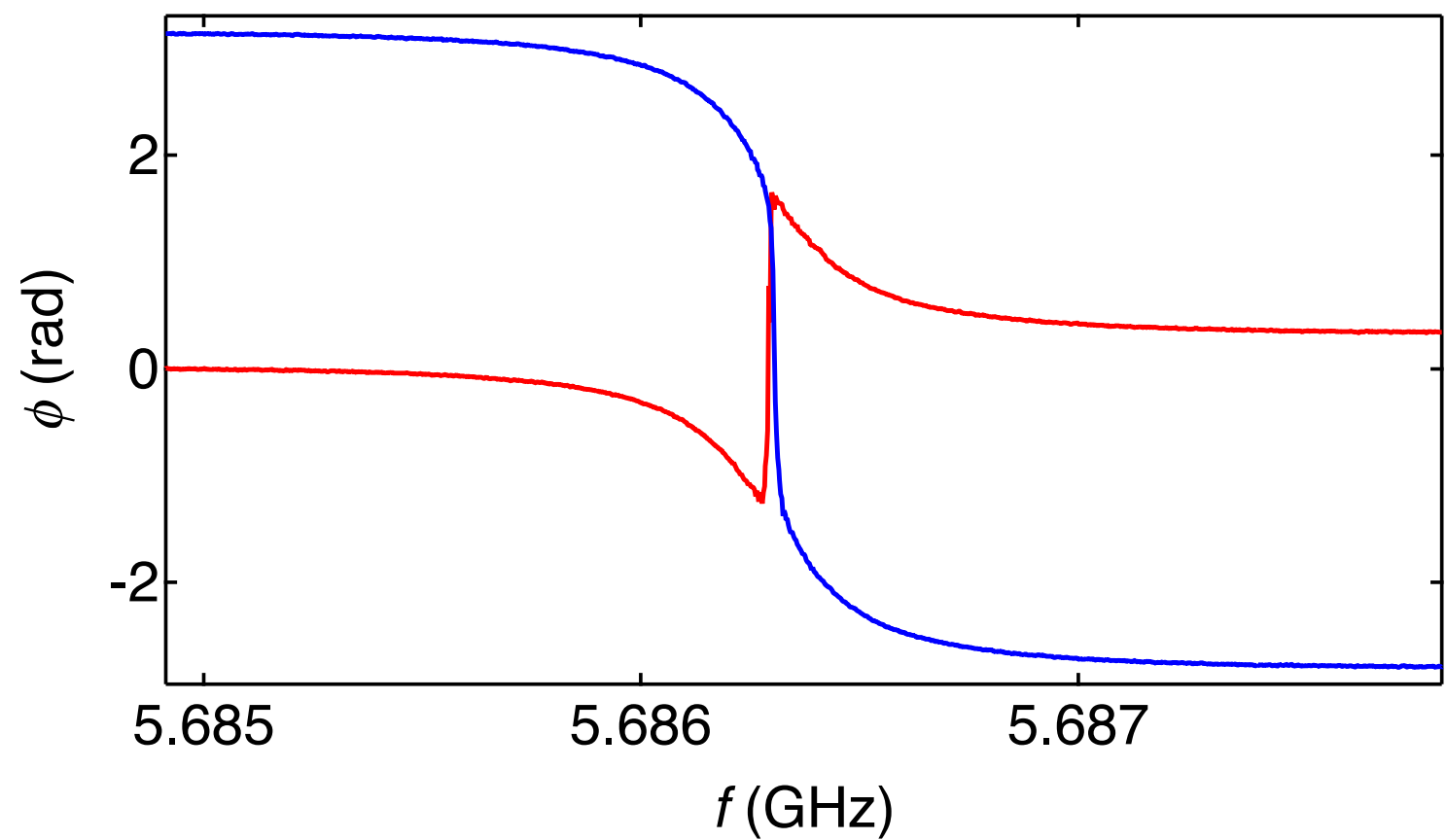
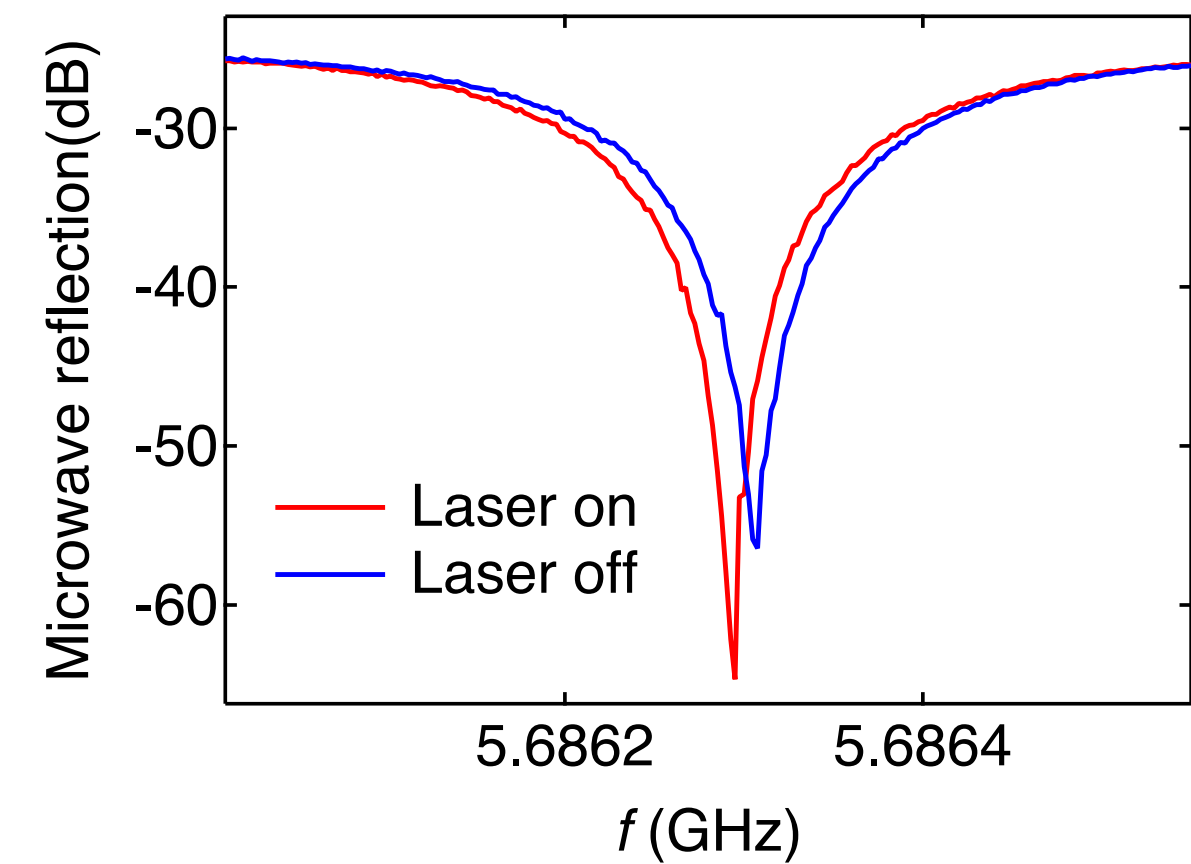
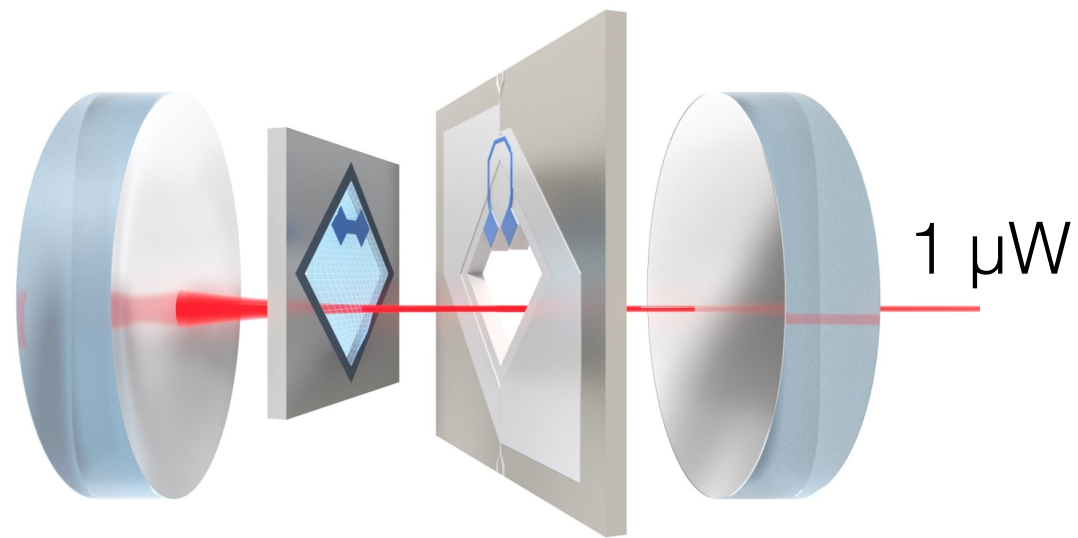


microwave linewidth: $\kappa_e = 2\pi \text{ 0.3 MHz}$

microwave efficiency: $\eta_e = \frac{\kappa_{e,\text{ext}}}{\kappa_e} = 0.5$

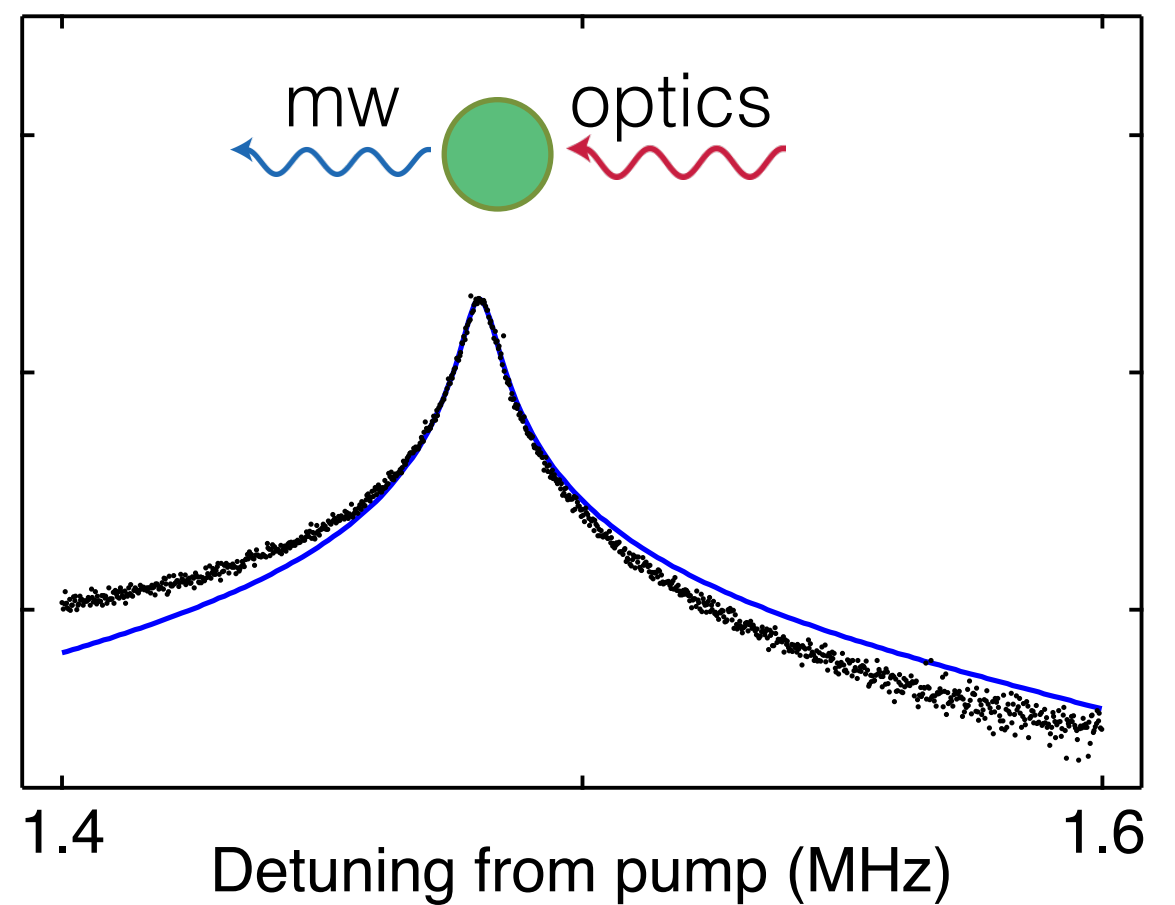
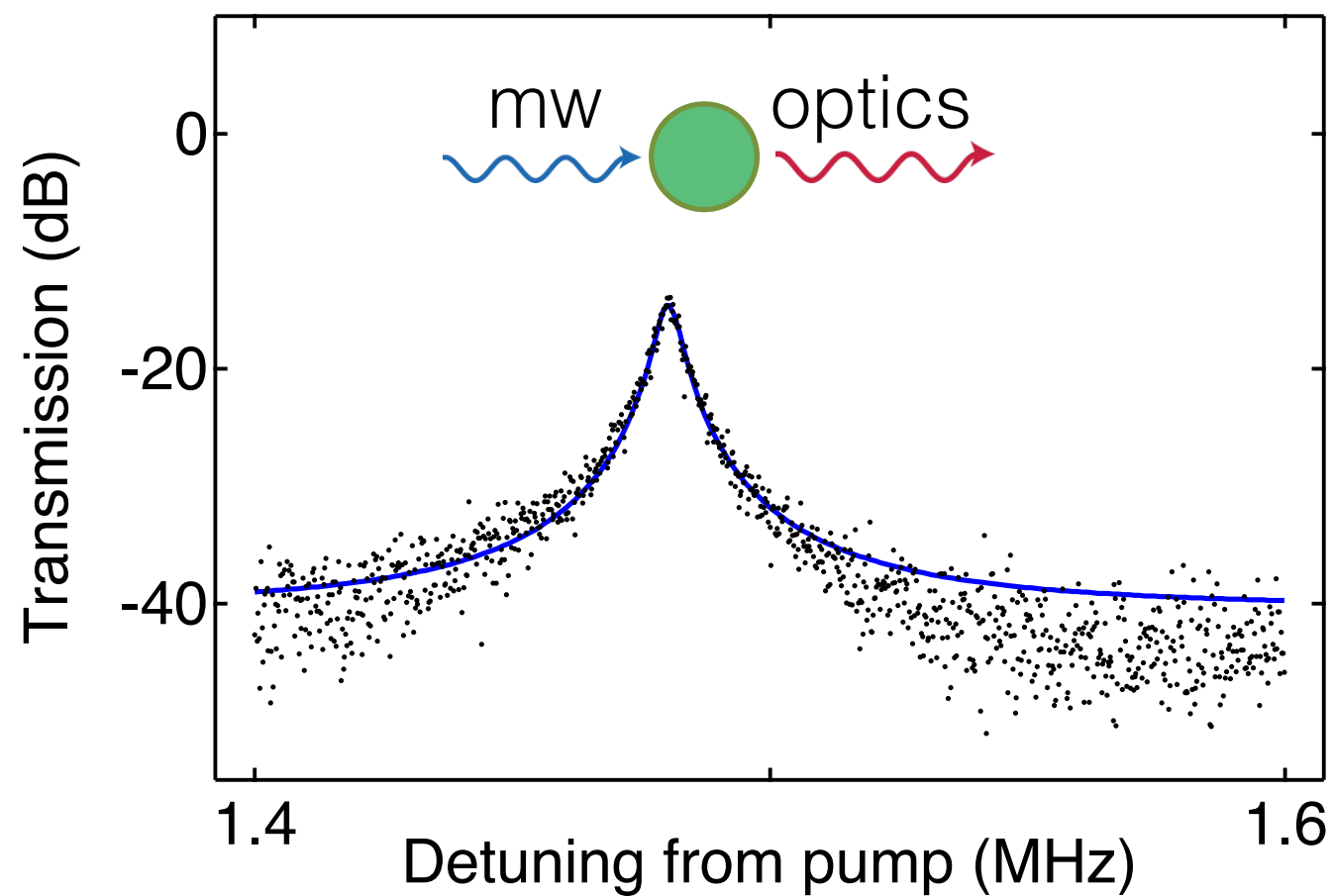
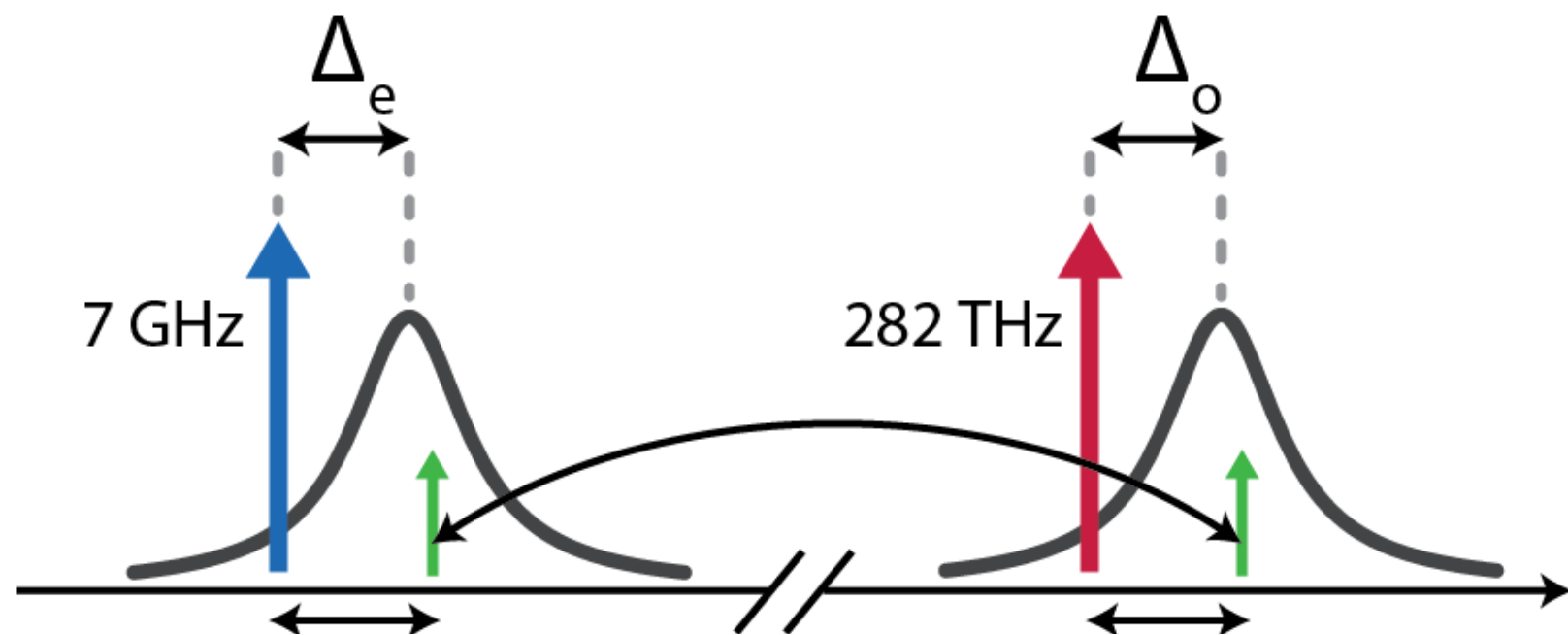
expect transfer efficiency: $\epsilon \cdot 35\%$

Effect of optical power on superconducting circuit

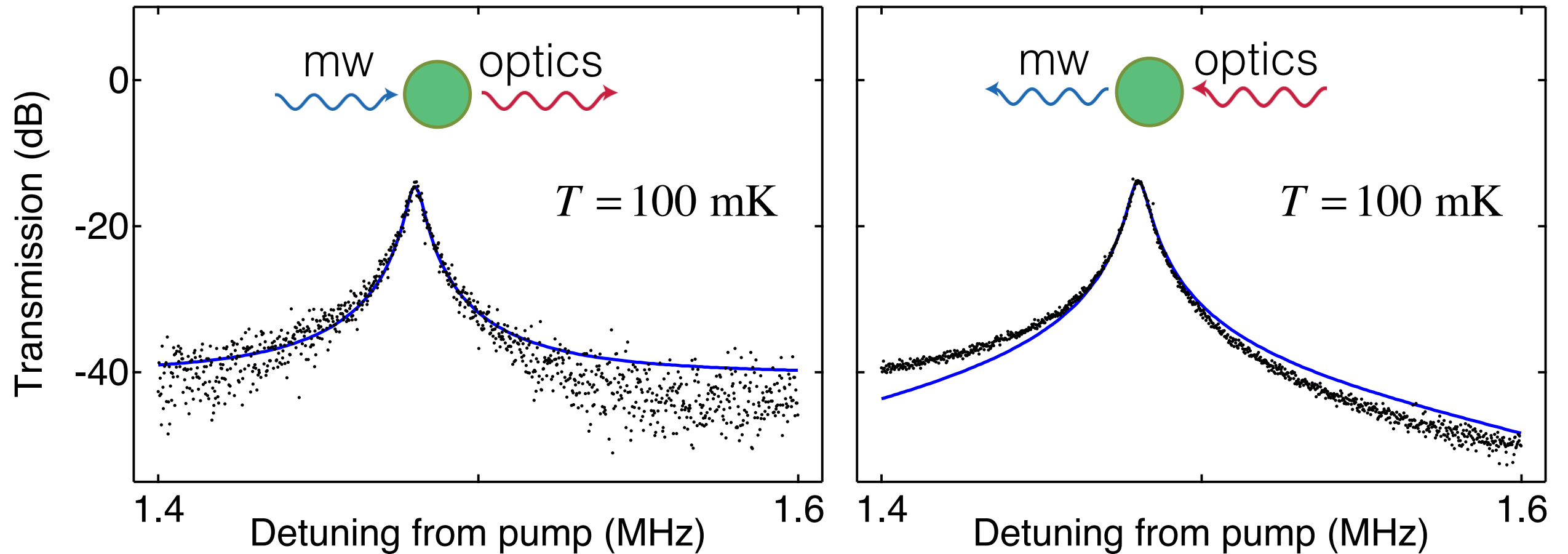


$1\ \mu\text{W}$ incident induces 20 kHz of microwave loss

State conversion at 100 mK



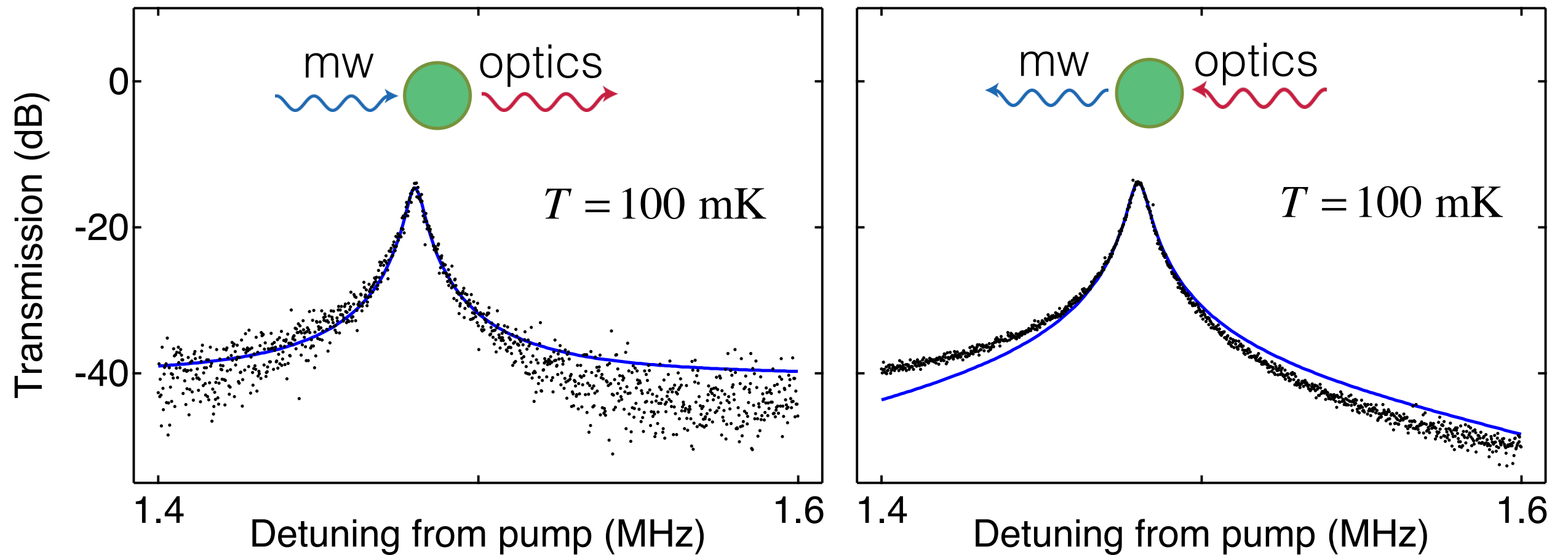
Efficiency of state conversion



apparent efficiency: $|t_1 t_2| = 0.038$

efficiency: $\frac{|t_1 t_2|}{\text{Gain}} = 3.5\%$

Main limitation: optical mode matching

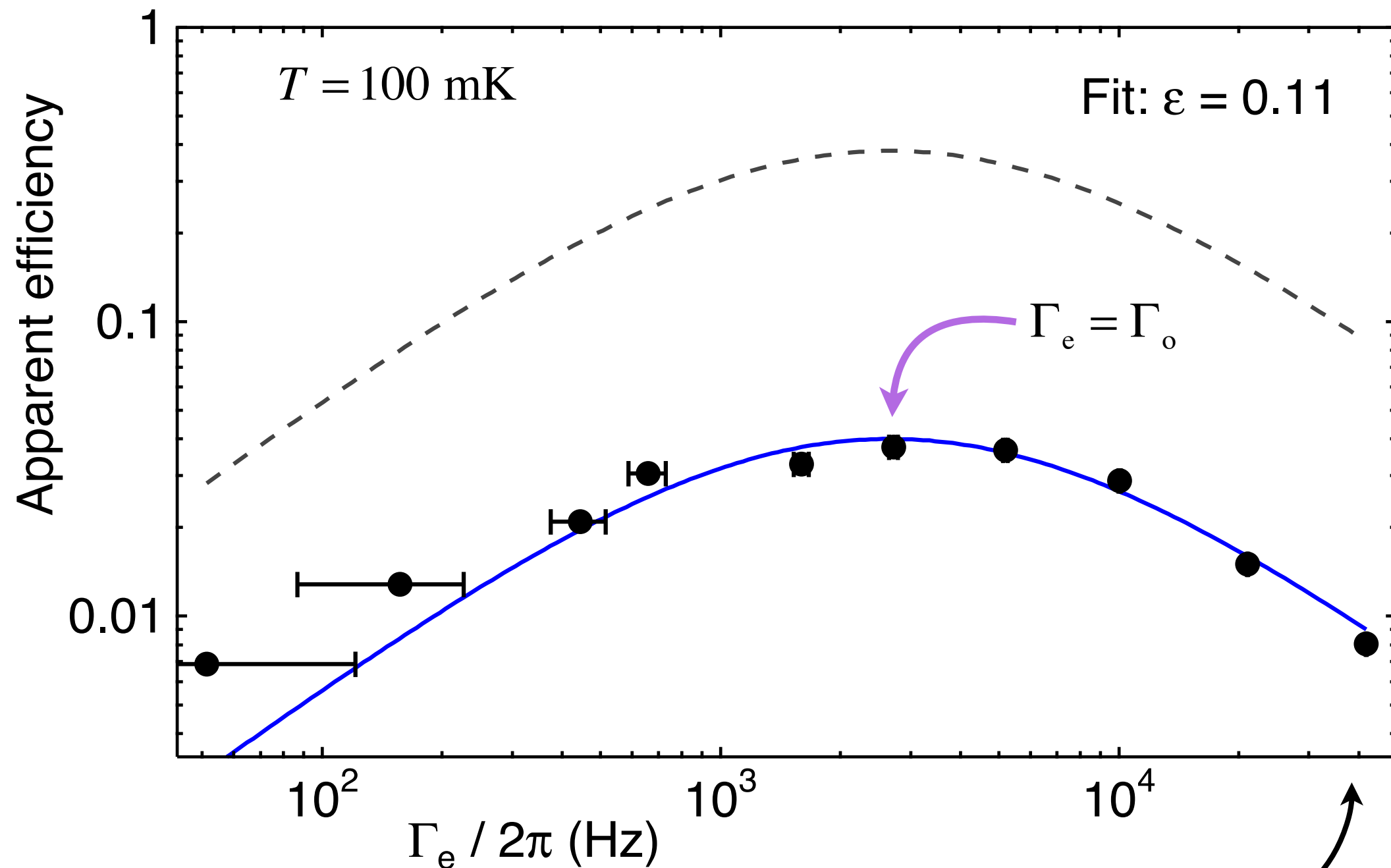


expected efficiency: $\epsilon \cdot 35\%$

$$\text{efficiency: } \frac{|t_1 \cdot t_2|}{\text{Gain}} = 3.5\%$$

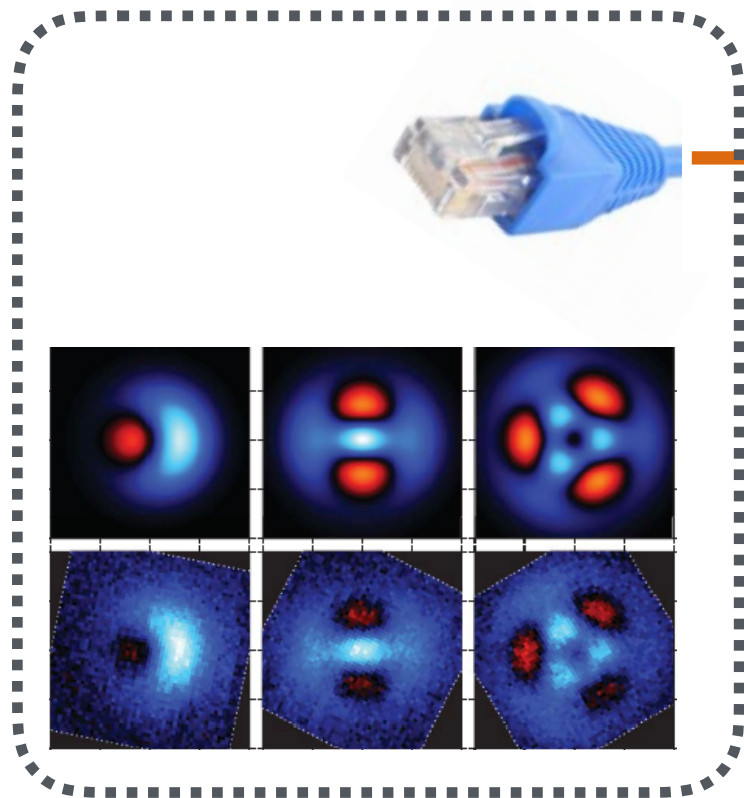
estimate mode matching: $\epsilon = 0.10$

Extracting the optical mode-matching factor



operation near the quantum regime: $\frac{C_o}{n_{\text{th}}} = 0.4$ $\frac{C_e}{n_{\text{th}}} = 5.4$

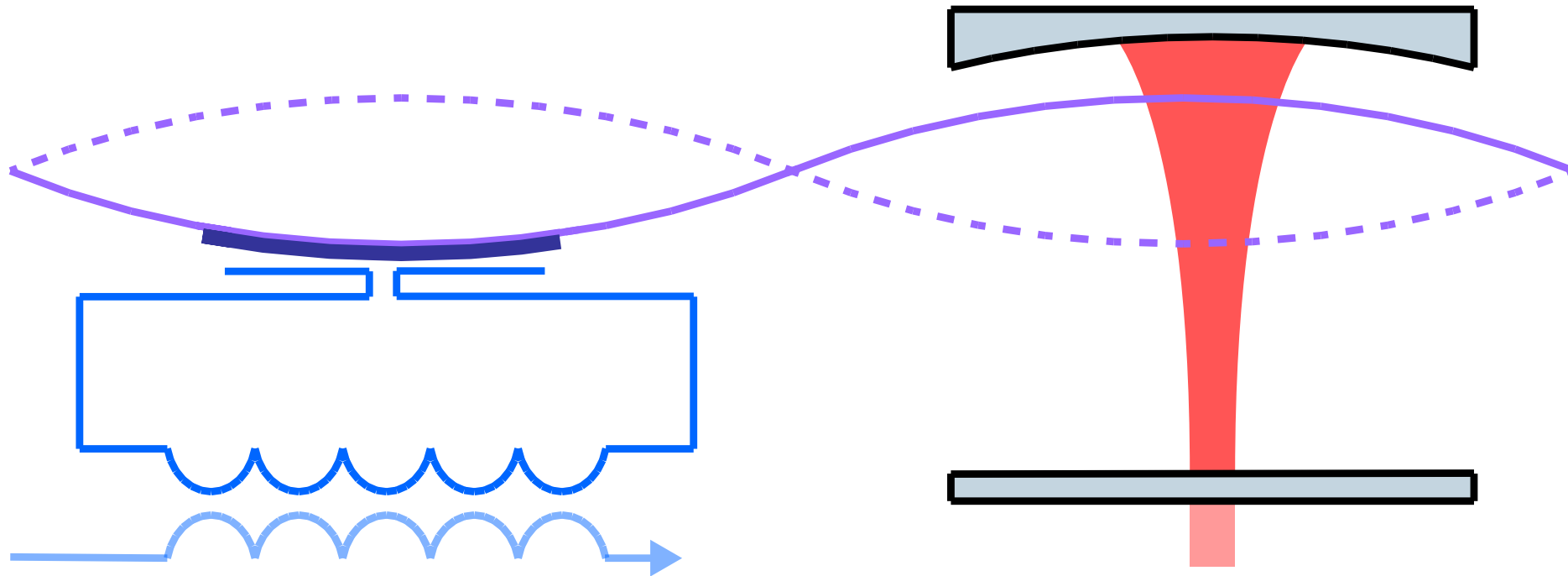
What is the first quantum experiment we can do?



$$\frac{C_o}{n_{\text{th}}} = 0.4$$

$$\frac{C_e}{n_{\text{th}}} = 5.4$$

Microwave-optical two-mode squeezing

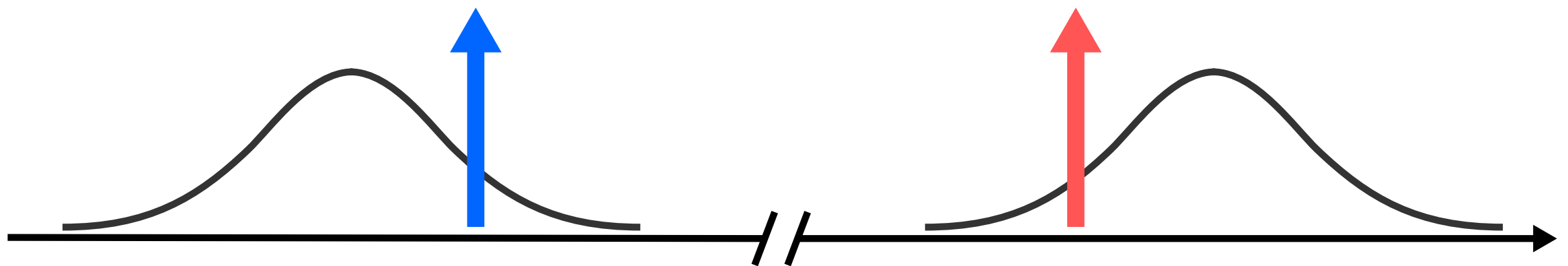


$$H_{\text{int}} = \hbar g_0 a_{\text{mw}}^\dagger a_{\text{mech}}^\dagger + \text{h.c.}$$

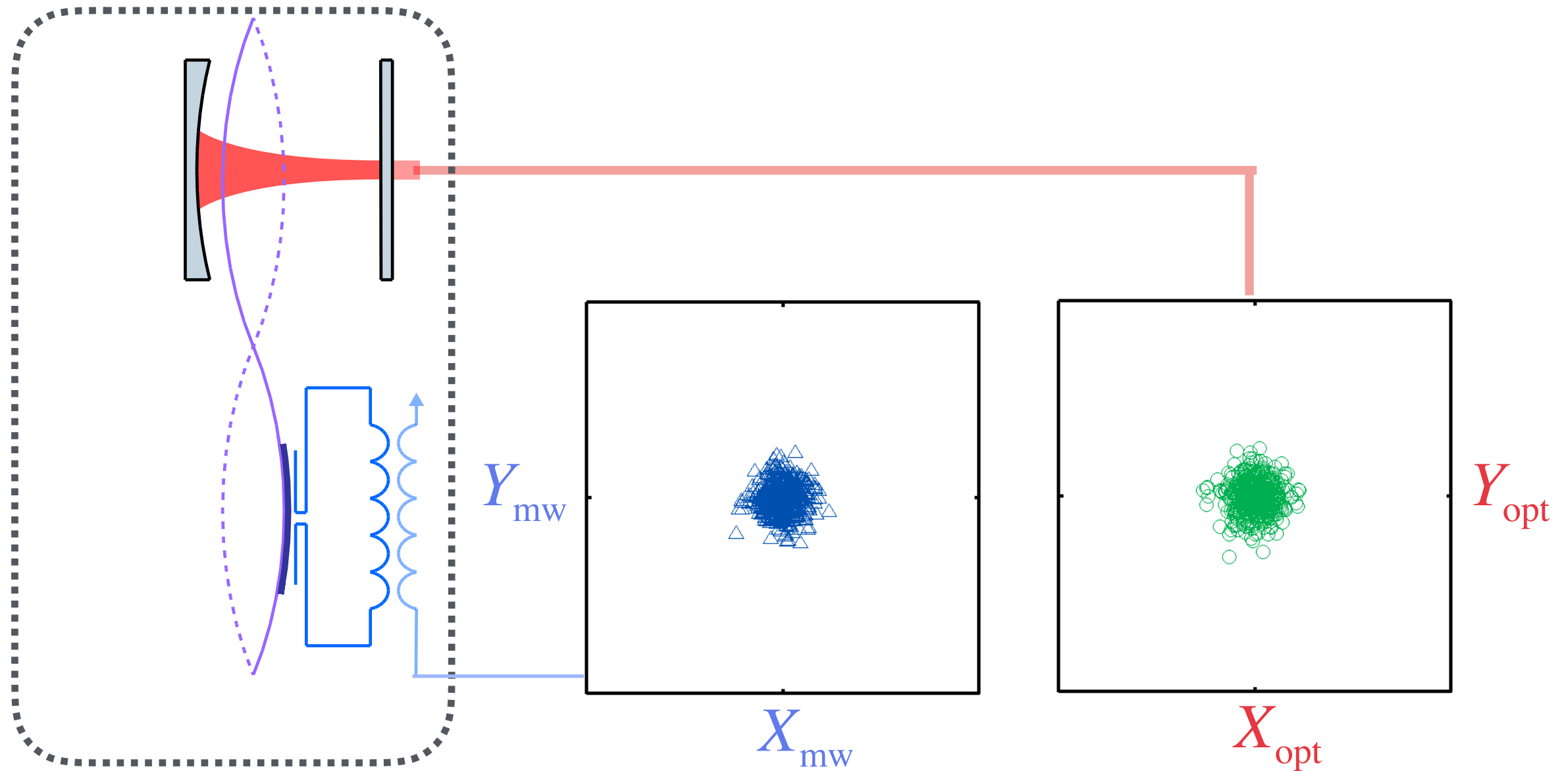
mw-mech entanglement

$$H_{\text{int}} = \hbar g_0 a_{\text{mech}} a_{\text{opt}}^\dagger + \text{h.c.}$$

swap mech to optics

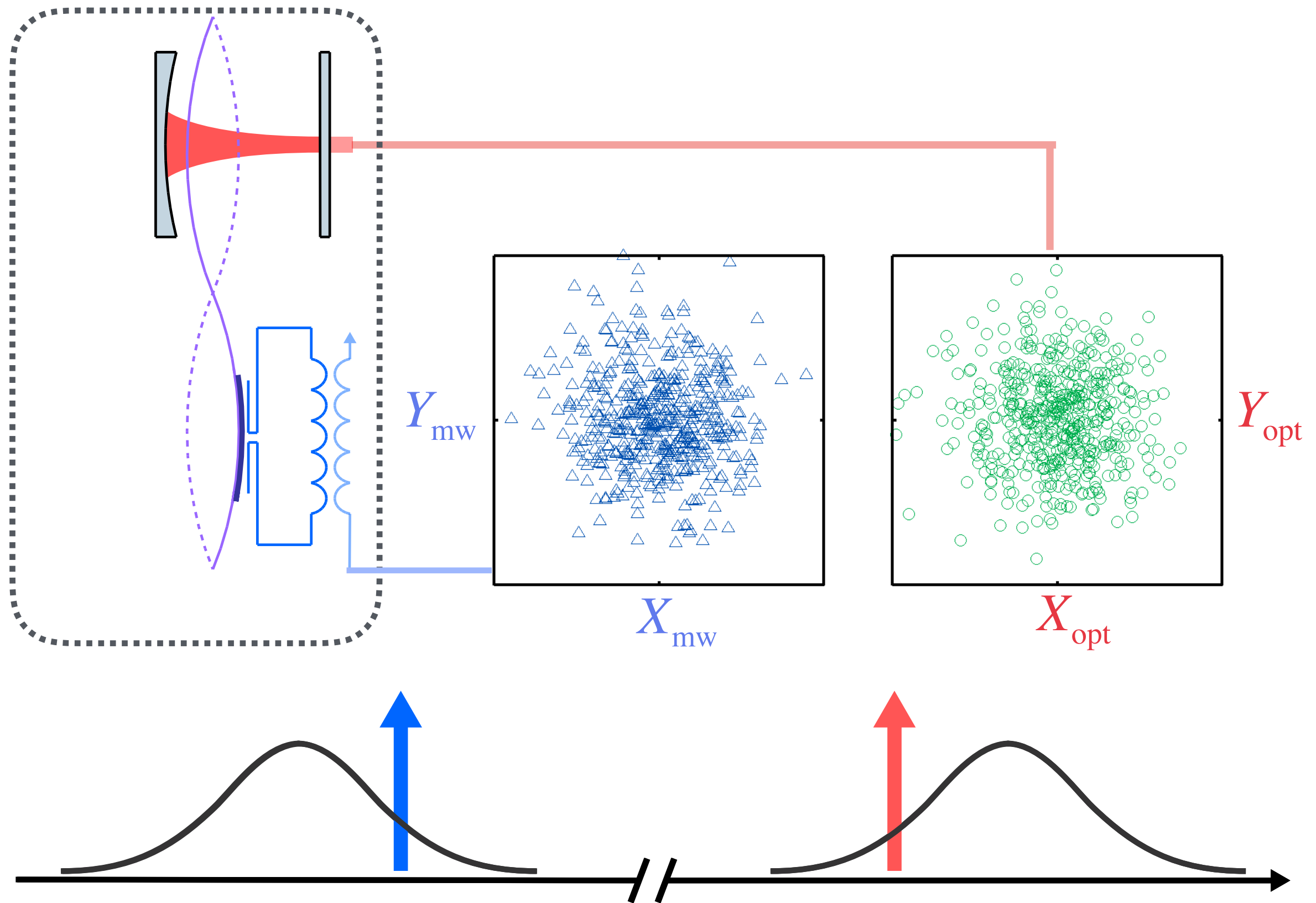


Two-mode squeezing

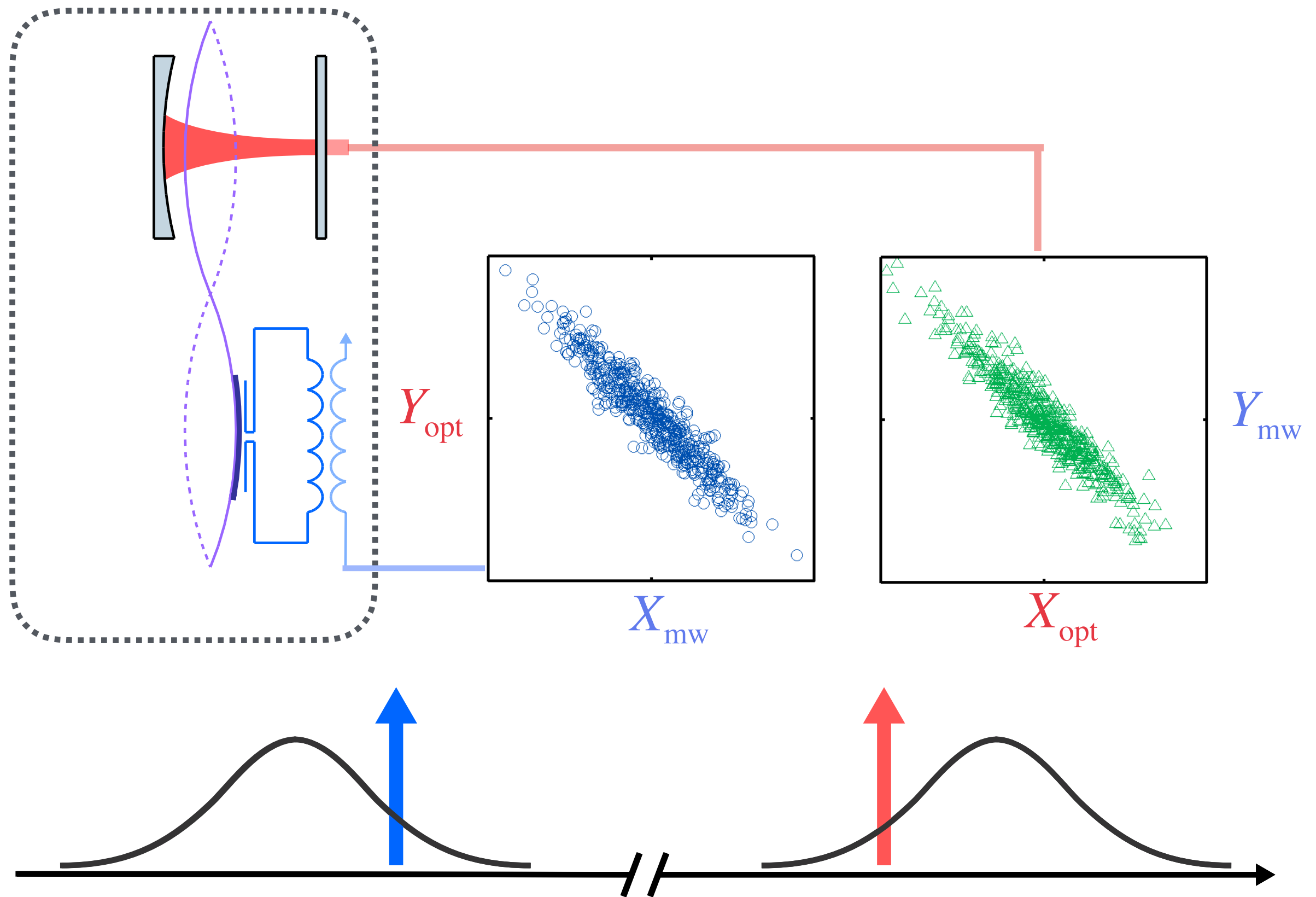


$$\begin{array}{c}
 \text{Gaussian curve} \\
 \hline
 H_{\text{int}} = \hbar g_0 a_{\text{mw}}^\dagger a_{\text{mech}}^\dagger + \text{h.c.}
 \end{array}
 \quad
 \begin{array}{c}
 \text{Gaussian curve} \\
 \hline
 H_{\text{int}} = \hbar g_0 a_{\text{mech}} a_{\text{opt}}^\dagger + \text{h.c.}
 \end{array}$$

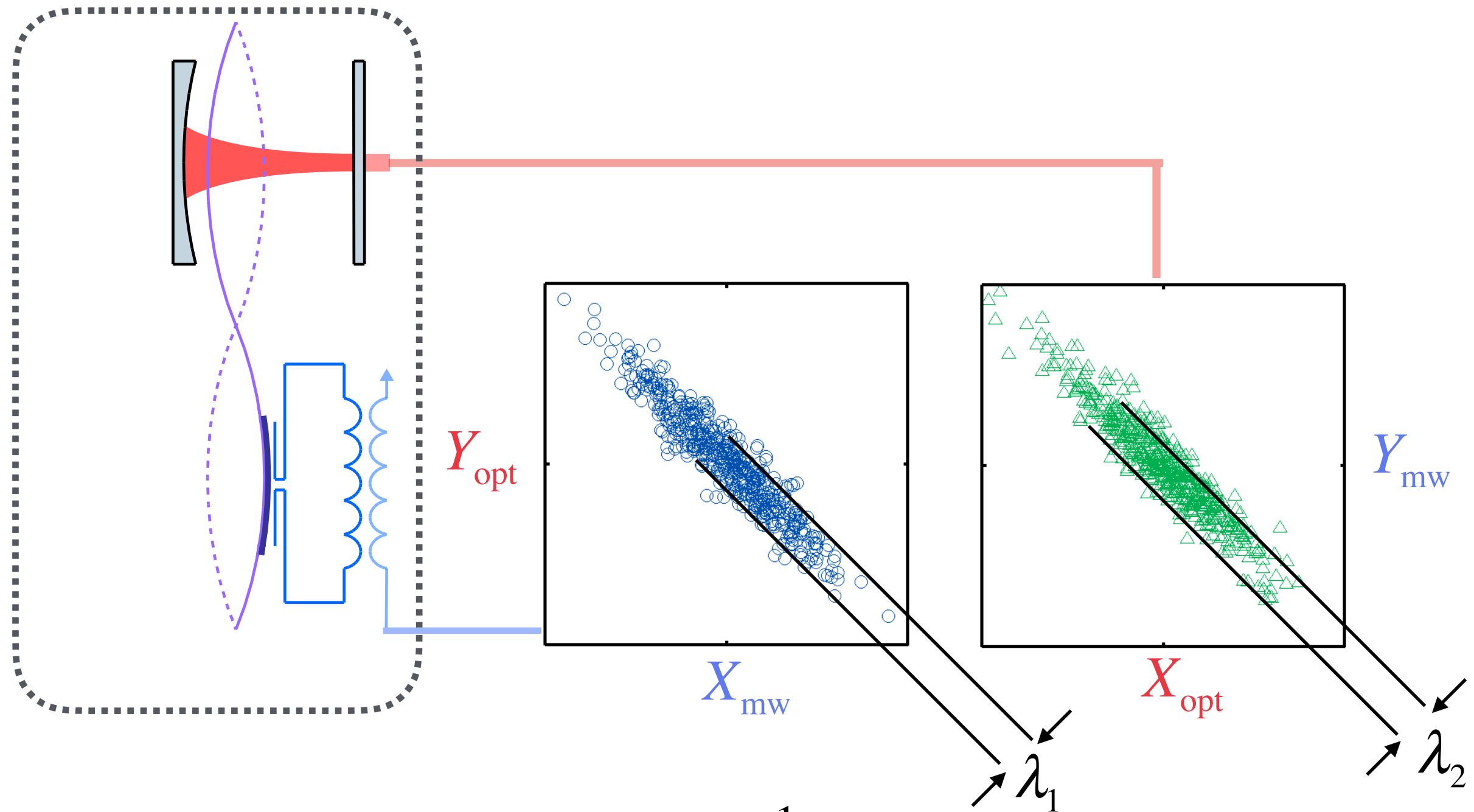
Two-mode squeezing



Two-mode squeezing



Two-mode squeezing



two-mode squeezing: $\lambda_1, \lambda_2 < \frac{1}{2}$

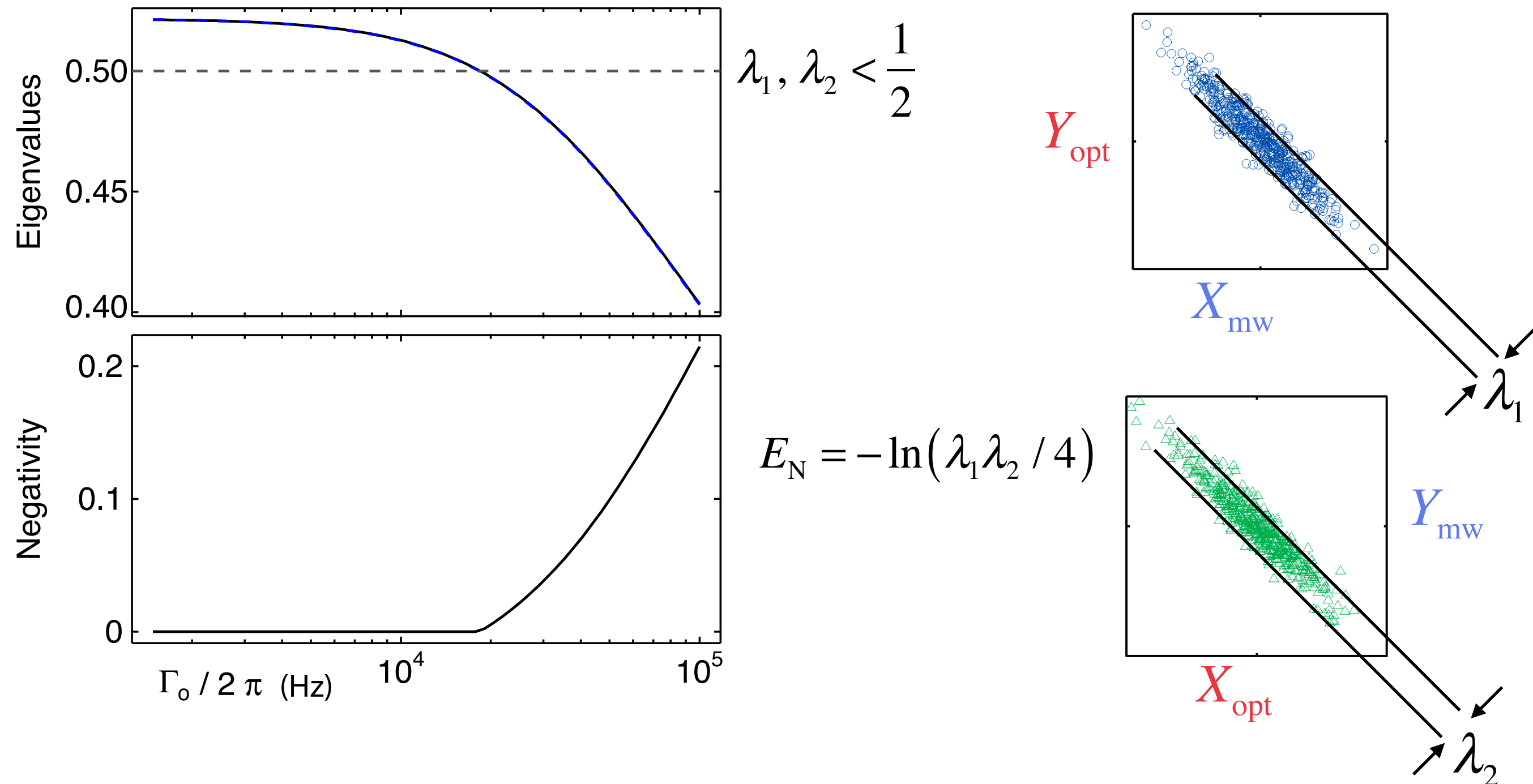
entanglement measure: $E_N = -\ln(\lambda_1 \lambda_2 / 4)$

Two-mode squeezing: quantitative expectations

Theory from: Genes, Mari, Tombesi, Vitali PRA **78** (2008)

Barzanjeh, Abdi, Milburn, Tombesi, Vitali PRL **109** (2012)

Equations of motion + in/out theory $\longrightarrow$ spectral density $\longrightarrow$ covariance matrix



Summary

- Classical conversion in a dilution refrigerator
- Operation near quantum regime
- Microwave-optical entanglement within reach

